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IN THE INTERPLANETARY MEDIUM: II

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## ABSTRACT

An extensive study of the dynamic, non-shock properties of the micro-scale fluctuations (scale lengths of .01 a.u. and less) in the interplanetary medium has been made using plasma and magnetic field data from Mariner V (Venus 1967). The observational results of the study are:

(1) large amplitude, non-sinusoidal Alfvén waves propagating outward from the sun with a broad wavelength range from  $10^3$  to  $5 \times 10^6$  km dominate the microscale structure at least 50 percent of the time; the waves frequently have energy densities comparable both to the unperturbed magnetic field energy density and to the thermal energy density; (2) the purest examples of these outwardly propagating Alfvén waves occur in high velocity solar wind streams and on their trailing edges (where the velocity decreases slowly with time). In low velocity regions Alfvén waves are also outwardly propagating, but usually have smaller amplitudes than in the fast streams, and tend to be less pure in the sense that they are more strongly intermixed with structures of a non-Alfvénic and possibly static nature; (3) the largest amplitude Alfvénic fluctuations are found in the compression regions at the leading edges of high velocity streams where the velocity increases rapidly with time; these regions may contain significant amounts of inwardly propagating or non-Alfvénic wave modes; (4) power spectra of the interplanetary magnetic field in the frequency range from  $1/(107 \text{ min.})$  to  $1/(25.2 \text{ sec.})$  have frequency dependencies of  $f^{-1.5}$  to  $f^{-2.2}$ ; the spectra with slower fall-offs tend to be associated with higher temperature regions; (5) the microscale magnetic field fluctuations have on the average a 5:4:1 power anisotropy in an orthogonal coordinate system whose axes are  $(\underline{e}_B \times \underline{e}_R, \underline{e}_B \times (\underline{e}_B \times \underline{e}_R), \underline{e}_B)$ , where  $\underline{e}_B$  is a unit vector in the average field direction

and  $\hat{e}_R$  is a unit vector radially away from the sun; this anisotropy tends to be strongest (6:3:1) in the compression regions at the leading edges of high velocity streams; (6) presumably magnetoacoustic wave modes occur, but they have not been identified, and, if present, have a small average power of the order of 10 percent or less of that in the Alfvén mode.

These observations are organized on the basis of a model of the solar wind velocity structure. Most of the Alfvén waves in the interplanetary medium seem likely to be the undamped remnants of waves generated at or near the sun. The high level of wave activity in high velocity, high temperature streams can be interpreted as evidence for the extensive heating of these streams by wave damping near the sun. The highest level of Alfvénic wave activity in the compression regions at the leading edges of high velocity streams may be due either to the amplification of ambient Alfvén waves in high velocity streams as they are swept into the compression regions or to the fresh generation of waves in these regions by the stream-stream collisions. The observed absence of the magnetoacoustic modes is evidence for their strong damping. The  $\hat{e}_B \times \hat{e}_R$  anisotropy is viewed as due to the partial conversion of the Alfvén waves to the damped magnetoacoustic modes as they are convected away from the sun; this process continually transfers energy from the microscale field fluctuations to the thermalized solar wind plasma.

## INTRODUCTION

The interplanetary medium is a highly conducting, essentially collisionless plasma with approximate equipartition between thermal and magnetic field energy densities. Spacecraft measurements of the fine scale structure of the medium (scale lengths of .01 a.u. and less) offer a unique opportunity to study the physics of such plasmas observationally. Of particular astrophysical interest are their wave and turbulence properties. When spacecraft data from interplanetary space were first obtained eight or more years ago, the fine or microscale structure of the medium was found to be quite irregular, and it seemed extremely plausible that many of the features would propagate as Alfvén or magnetoacoustic waves. From statistical analyses of the Mariner 2 magnetometer and plasma data, Coleman [1967, 1968] concluded that fluctuations with periods in the spacecraft frame from 10 to  $10^4$  sec. were largely due to Alfvén waves. However, the only example in which such waves were specifically identified was in a two hour segment of Mariner 2 data where Unti and Neugebauer [1968] demonstrated the existence of a quasi-sinusoidal Alfvénic waveform with a period in the spacecraft frame of about 30 minutes. It was not possible from the statistical analyses to distinguish periods in which Alfvén waves dominated the fluctuations from periods when they did not, and Coleman [1968] arrived at a model for the interplanetary medium that differs significantly from that proposed below.

More recent studies of the microscale structure [Siscoe, et.al., 1968; Burlaga, 1968, 1969] have not emphasized the existence of wave-like fluctuations in the solar wind. They are primarily concerned with the properties of abrupt discontinuities in the direction of the interplanetary magnetic

field; such discontinuous changes are tentatively attributed to the presence of convected static structures which do not propagate in the rest frame of the wind. It has been argued [Sari and Ness, 1969; Ness, 1969] that most of the interplanetary microscale fluctuations are not due to the existence of plasma waves, but rather to the convection past the spacecraft of equilibrium solar wind regions separated by tangential discontinuities.

Data returned from Mariner 5 (Venus 1967) conclusively demonstrate that plasma waves are a major source of interplanetary microscale fluctuations. Preliminary analysis of simultaneous Mariner 5 magnetometer and plasma data indicated that much of the time during June-November 1967 large amplitude Alfvén waves propagating outward from the sun dominated the microscale structure of the interplanetary medium [Belcher, Davis, and Smith, 1969, hereafter referred to as I]. The purpose of the present paper is to present a more extensive analysis of the microscale fluctuations, including vector (rather than merely single components) correlations between the magnetic field and the bulk velocity, which strongly supports this initial conclusion. Various additional properties of the Alfvén waves, such as spectral dependence and characteristic patterns of occurrence, are considered. Also, we study anisotropies in the magnetic field microscale fluctuations using the variance tensor method, an approach which is essentially independent of the coordinate system. The two major sections of the paper are, first, primarily a quantitative discussion of the observational properties of the Alfvén waves, and, second, a qualitative discussion of possible physical mechanisms which may produce these properties.

Mariner 5 was in operation from June 14, 1967 to November 21, 1967. Magnetic measurements were made by a low-field, vector, helium magnetometer

[Connor, 1968]; three vector field readings were obtained every 12.6 seconds until July 24 (day 205) and every 50.4 seconds after that time. The vector  $\underline{B}$  has been resolved into solar polar coordinates. The positive R direction is radially outward from the sun; the T direction is parallel to the solar equatorial plane and positive in the direction of planetary motion; the N direction is northward along  $\underline{R} \times \underline{T}$  so that RTN is right-handed. The plasma detector, a modulated grid Faraday cup [Lazarus et al., 1967], points at the sun and measures positive ion currents in 32 energy levels from 40 to 9400 ev, with a sampling period of 5.04 minutes at the high data rate and 20.16 minutes at the low rate.

The spacecraft field was determined by the variance method [Davis et al., 1968]. Abrupt changes in the spacecraft field estimate occurred at the midcourse correction ( $\Delta B_s \approx 1.4\gamma$ ), at the shift from the cavity amplifier to the TWT amplifier ( $\Delta B_s \approx .5\gamma$ ), and at three other similar events ( $\Delta B_s \approx .5\gamma$ ). Other than at these five points, the spacecraft field estimate was never changed more than  $.06\gamma$  from one day to the next, with only one spacecraft field correction each day. The spacecraft field was constant for long periods of time, with occasional slow linear drifts accounting for at most  $.06\gamma/\text{day}$  corrections.

The highest frequencies which have been studied using the Mariner 5 data are low compared to the interplanetary proton gyro frequency ( $\sim 1$  cps). Thus the relevant plasma physics is that of a fully ionized collisionless gas at frequencies low compared to gyro frequencies and at scale lengths long compared to gyro radii. We shall make the standard MHD assumption in interpreting the observations, as it seems quite adequate for a description

of the observed wave properties of the medium. Throughout, we use the term wave in a broad sense. In many instances the terms Alfvénic turbulence or rotational discontinuity might be more appropriate, although neither is fully descriptive of the phenomenon. In all cases, the term wave is used to apply to dynamic, non-shock structures, almost always non-sinusoidal and nonperiodic, which propagate in the rest frame of the solar wind.

First, let us summarize some of the well-known difficulties in the interpretation of spacecraft data. The plasma is convected past the spacecraft with a velocity ( $\sim 400$  km/sec) that is high compared to the characteristic MHD propagation speeds ( $\sim 50$  km/sec). Thus, all MHD disturbances are convected outward whatever their true direction of propagation in the rest frame of the plasma. Observed variations are primarily due to the convection past the spacecraft of spatial structures which may be either static and "frozen-in" or dynamic and slowly propagating. In the frame of the wind, the two classes of structures have substantially different properties, different origins, and different physical natures; in the spacecraft frame, they may be quite difficult to distinguish on the basis of either magnetometer or plasma data alone. As we shall see, an identification can usually be made on the basis of a careful study of both magnetic field and plasma data. Unless otherwise specified, time and frequencies given hereafter refer to the spacecraft frame; these must be Doppler shifted to yield wavelengths and frequencies in the rest frame of the wind. For example, a wave structure propagating outward from the sun with the Alfvén velocity  $V_A$  superposed on the wind velocity  $V_W$  and having an apparent period  $T$  in the spacecraft frame has a wavelength of  $T(V_W + V_A)$  and period of  $T \left[ (V_W/V_A) + 1 \right]$  in the rest frame of the wind.

## ANALYSIS OF OBSERVATIONS

### Vector Correlations

Consider a wave propagating in an homogeneous plasma that is moving with an average bulk velocity  $\underline{v}$ . Let  $\underline{v}$  be the perturbations in velocity due to the wave,  $\underline{B}_0$  be the static background magnetic field,  $\underline{b}$  its fluctuations,  $N$  the proton number density,  $N_\alpha$  the alpha number density, and  $m_p$  the mass of the proton, all in cps and Gaussian units unless other units are explicitly stated. Then, for an Alfvén wave

$$(1) \quad \underline{b} = \pm D_A \underline{v}$$

$$D_A = \left[ 4\pi m_p (N + 4N_\alpha) \right]^{1/2} \Theta_A \frac{\text{gauss}}{\text{cm sec}^{-1}} = \frac{(N+4N_\alpha)^{1/2}}{21.8} \Theta_A \frac{\text{gamma}}{\text{km sec}^{-1}}$$

where  $\Theta_A$  is a correction factor

$$\Theta_A = \left[ 1 - \frac{4\pi(p_{\parallel} - p_{\perp})}{B_0^2} \right]^{-1/2}$$

to be used in case one is dealing with an anisotropic plasma where  $p_{\parallel}$ , the pressure parallel to  $B_0$ , is larger than  $p_{\perp}$ , the pressure normal to  $B_0$  [Parker 1957; I]. If  $\underline{k}$  is the propagation vector, the sign in (1) is the sign of  $-\underline{k} \cdot \underline{B}_0$ ; i.e., when  $\underline{k}$  has a positive (negative) component along  $B_0$ ,  $\underline{b}$  is anti-parallel (parallel) to  $\underline{v}$ . Preliminary radial velocity data provided by the MIT plasma group were combined with magnetometer data in paper I to demonstrate that much of the time in the solar wind the R component of (1) was satisfied. This correlation was interpreted as indicating that (1) was satisfied as a vector relation, and that Alfvén waves were responsible for the fluctuations. The MIT group has now completed a more

extensive reduction of their data, including estimates of proton thermal velocities, alpha particle densities, and preliminary estimates of all three components of the proton bulk velocities. Examination of the variations in the tangential and normal components of the wind velocity ( $V_T$  and  $V_N$ , respectively, in solar polar coordinates) during periods of previously identified Alfvén waves establishes that (1) is in fact a valid vector relation. Figure 1 shows the variations in the plasma probe and magnetometer data for a 24 hour period starting at 0400 on day 166. For each component, the average of that component over the 24 hour period has been subtracted; thus, the plots show the fluctuations about the average ( $\langle B_R \rangle = -1.9\gamma$ ,  $\langle B_T \rangle = 1.4\gamma$ ,  $\langle B_N \rangle = 1.2\gamma$ ,  $\langle V_R \rangle = 427$  km/sec;  $\langle V_T \rangle$  and  $\langle V_N \rangle$  have not yet been corrected for aberration due to the spacecraft motion). The two lower curves on the plot are proton number density and magnetic field strength ( $\langle B \rangle = 5.3\gamma$ ,  $\langle N \rangle = 5.4 \text{ cm}^{-3}$ ). This period is one of the better examples of the waves and illustrates their most characteristic features -- close correlation between  $\tilde{b}$  and  $\tilde{v}$ , variations in  $\tilde{b}$  comparable to the field strength, and relatively little variation in field strength or density. In this case, the average magnetic field is inward along the spiral and the correlation between  $\tilde{b}$  and  $\tilde{v}$  is positive; when the magnetic field is outward, the correlation in periods of good waves is negative. This indicates outward propagation (see equation (1)).

The scale ratio used for plotting the magnetic field and velocity variations in Figure 1 correspond to a value of  $D_A^{-1}$  of  $6.4 \text{ km sec}^{-1}/\gamma$ . This was determined by the condition that when this ratio is used for a fixed area plot of  $v_R$  versus  $b_R$  for all the data, the sum of the squares of the perpendicular distances from the points to a line of unit slope is minimized. (Mathematically this gives  $D_A^{-1} = \sigma_{v_R}/\sigma_{b_R}$ , the ratio of the

standard deviations.) The average values of  $N$  and  $N_\alpha$  during this period are  $5.4 \text{ cm}^{-3}$  and  $0.4 \text{ cm}^{-3}$ , respectively; thus equation (1) with  $\Theta_A = 1$  gives  $D_A^{-1} = 8.2 \text{ km sec}^{-1}/\gamma$ . We feel that the discrepancy between this predicted value and the observed value of 6.4 is significant and probably is due to the anisotropy in the pressure. This requires that  $4\pi(p_{\parallel}-p_{\perp})/B_0^2$  be 0.40. The average during this period of  $(2kT_p/m_p)^{1/2}$ , the most probable proton velocity, was observed to be 47 km/sec, which corresponds to  $4\pi p_p/B_0^2 = 0.5$ , where  $p_p$  is the mean proton pressure. With reasonable values of the electron and alpha pressures and of the pressure anisotropy [Hundhausen et al., 1967], the required value of  $\Theta_A$  seems entirely reasonable. On other occasions when  $\beta = 8\pi p_p/B_0^2$  is smaller, values of  $\Theta_A$  closer to unity would be expected.

#### Waves Versus Discontinuities

Figure 2 is an expanded plot of three particular ten minute periods indicated on Figure 1, where the crosses are the basic magnetometer data (one reading in approximately four seconds) and the lines are the plasma data (one per 5.04 min), scaled in the same ratio as in Figure 1. On this time scale, the waves may be either gradual (2b) or discontinuous (2a,2c), with abrupt changes within 4 seconds. As discussed below, we feel that all three examples are Alfvénic, with continuous magnetic field lines, but with a discontinuity in direction in cases 2a and 2c. Such abrupt changes occur at a rate of about one per hour, and are enmeshed in more gradual changes.

The visual appearance of the field fluctuations is qualitatively different on the time scales of Figures 1 and 2. With the scale used in Figure 2, the most prominent structures are the abrupt changes which tend to be preceded and followed by field values that appear nearly constant. For example, the structure in Figure 2a is more striking than that in 2b

even though both have about the same total change over the ten minute period, and both appear very similar in Figure 1. On the time scale of Figure 1, the genuine high frequency abrupt changes do not stand out because they are indistinguishable from large smooth changes when the data are averaged over 5.04 minute intervals, and because the field no longer appears to remain steady before and after the jumps. Because the abrupt changes are the most visually striking features when field data are plotted at a high time resolution, even though they are relatively infrequent and not necessarily intrinsically different from the smoother variations, numerous studies have been made of their structure and frequency of occurrence [ Siscoe et al. 1968, Burlaga 1968, 1969 ]. These authors have tentatively concluded that most of the discontinuities in the solar wind are tangential (non-propagating). In fact, it has been suggested [ Ness, 1969 ] that the fluctuations in Figure 1 are not dynamic structures propagating in the rest frame of the solar wind, but rather are an ensemble of spatially convected static MHD discontinuities in equilibrium. Since this point is of major importance in the interpretation of interplanetary magnetic field fluctuations, we discuss it in some detail.

Consider the two non-propagating discontinuities in the isotropic MHD approximation, the contact and the tangential [ Landau and Lifshitz, 1960 ]. The magnetic field is continuous across the contact surface, which is of no interest to us, but both plasma and field parameters can change across the tangential discontinuity. Let n and t be subscripts denoting components normal and tangential, respectively, to the discontinuity surface and let [A] denote the change in A across the surface. A tangential discontinuity is characterized by  $B_n = 0$ ,  $V_n = 0$ , arbitrary and unrelated  $[V_t]$  and  $[B_t]$ , and any change in pressure and field strength subject to the condition

$[p + B^2/8\pi] = 0$ . By constructing a series of special tangential discontinuities, all having continuous density and field strength, with the plane of the discontinuity so chosen that  $B_n = 0$  on both sides, and with  $[B_t]$  and  $[V_t]$  related by equation (1) with  $\theta_A = 1$  (where the sign is consistent from discontinuity to discontinuity and changes with the polarity), we can in fact make a structure such as in Figure 1 which is static. None of these special conditions are required, but they are allowed by the tangential discontinuity equations. However, it is not clear what physical mechanism would cause such a configuration in the first place, and while it is possible to explain any one discontinuity in this way, it is hard to fit together a large number unless their shear planes are all parallel. On the other hand, the Alfvén wave hypothesis accounts for all of the observed properties in a straight forward manner. When sufficiently sharp crested, an Alfvén wave can be termed a rotational discontinuity. Such a discontinuity has continuous density and field strength,  $B_n$  is non-zero and continuous, and  $[B_t]$  and  $[V_t]$  are related by equation (1) with  $\theta_A = 1$ . The only special conditions needed to produce a data sequence as in Figure 1 is that all the Alfvén waves propagate outward.

The fluctuations in Figure 1 are thus viewed as purely Alfvénic, with occasional sharply crested Alfvén waves enmeshed in more gradual variations. This interpretation is in sharp contrast to the non-propagating, filamentary model of the microscale structure consisting of equilibrium regions of differing properties separated by tangential discontinuities and convected outward from the sun by the solar wind. Periods such as in Figure 1 are usually found in high velocity streams and on their trailing edges; they can last as long as three days ( $\sim 7$  a.u. of gas), and almost every discontinuity in that time appears to be a sharply crested Alfvén wave. We do

not mean to imply that all discontinuities in the solar wind are Alfvénic, as this is obviously not the case, but it appears that a high percentage of them are, particularly in certain regions (as discussed below). Similarly, we feel that the filamentary or discontinuous model of the microscale structure is valid in many circumstances, but that it must be applied with care. Even a tentative identification of structures as dynamic or static must include a careful study of both magnetic field and plasma data.

#### Frequency of Occurrence and Direction of Propagation

It should be emphasized that the presence of the waves is very common, and tends to dominate the microstructure of the interplanetary medium. There are a total of about 25 days (a day being 24 consecutive hours) from the 160 day mission during which the Alfvén waves are as "pure" as those in Figure 1; such periods tend to occur in high velocity streams and on their trailing edges where typically the density is low and the temperature high. Other examples of the waves, in the presence of large scale velocity gradients, static structures, shocks, polarity reversals, etc., are less clean, but still recognizably present. The identification of the waves during such periods is based on a visual inspection of plots of simultaneous plasma and field data at high time resolution. Alfvén waves are adjudged to be present if there is substantial high frequency fluctuation in the magnetic field, a good high frequency correlation between  $B_R$  and  $V_R$  (low frequency correlations are influenced by slow linear trends), and relatively little high frequency fluctuation in density and field strength. In the following, we will state whether Alfvén waves are present or not on the basis of such comparisons of plasma and field data, although such data will not always be reproduced.

To obtain a rough statistical measure of the prevalence of the waves, we have examined the distribution of  $\rho$ , the correlation coefficient between  $B_R$  and  $V_R$  computed over six hour intervals throughout the entire mission. Six hour intervals dominated by outwardly propagating Alfvén waves will have high values of  $|\rho|$ , and  $\rho$  will have the same sign as  $-P$ , where  $P$  is the polarity of the average field direction (+1 for  $\langle \underline{B} \rangle$  outward along the spiral and -1 for  $\langle \underline{B} \rangle$  inward along the spiral). For the 416 six-hour intervals in the flight with more than 66 percent data return, 33 percent of the intervals had  $|\rho| \geq .8$  and 55 percent had  $|\rho| \geq .6$ . The sign of  $\rho$  correlates extremely well with the polarity of the field. Table 1 lists the percentage of the six-hour intervals with  $|\rho|$  in the indicated ranges for which  $\rho P$  is negative. Those six-hour intervals (112 out of 416) for which  $\langle \underline{B} \rangle$  was not within  $45^\circ$  of a  $45^\circ$  spiral angle are not included because of their poorly defined polarity. All but three of the remaining six-hour intervals with  $|\rho| \geq .8$  have  $\rho P < 0$ , indicating outwardly propagating waves. Inspection of the three six-hour intervals which are exceptions reveals that the high correlation and positive  $\rho P$  are not caused by inwardly propagating waves, but by slow linear trends during quiet times; such trends can cause a spuriously high value of  $|\rho|$  even when there are no wave-like or higher frequency fluctuations present. Thus, Alfvén waves in periods of high  $|\rho|$  are essentially always outwardly propagating.

Periods for which  $|\rho|$  is not as high ( $|\rho| < .8$ ) have  $\rho P < 0$  a large percentage of the time (see Table 1), but not as consistently as do periods of higher correlation. The smaller values of  $|\rho|$  could be caused by the presence of static structures, shocks, slow linear trends, etc., which can mask the effect of the correlation due to the waves. The intervals with  $\rho P > 0$  could be due to linear trends that cause a high value of  $|\rho|$  even

TABLE 1

Range of $ \rho $	No. and percent intervals in this range	Percent intervals with $\rho P < 0$
.0/.2	44 (14)	66
.2/.4	41 (14)	68
.4/.6	47 (15)	83
.6/.8	76 (25)	83
.8/1.0	96 (32)	97
<hr/>	<hr/>	<hr/>
.0/1.0	304 (100)	83

when no waves are present. They could also be due to the presence of inwardly propagating Alfvén waves. Suppose that we are studying microscale fluctuations which are exclusively due to an outwardly propagating Alfvén wave of amplitude  $A_+$  and an inwardly propagating Alfvén wave of amplitude  $A_-$ , with no cross correlation between the two waveforms; then it is easily shown that  $\rho P = (A_-^2 - A_+^2)/(A_-^2 + A_+^2)$ . For  $A_-^2/A_+^2 = 1/9$ ,  $\rho P = -.8$ , for  $A_-^2/A_+^2 = 1/3$ ,  $\rho P = -.5$ , and for  $A_-^2/A_+^2 = 1$ ,  $\rho P = 0$ . Thus, the presence of inwardly propagating Alfvén waves can significantly reduce  $|\rho|$  during periods of purely Alfvénic fluctuations, and it is possible that six-hour intervals for which  $|\rho| \leq .8$  have inwardly propagating Alfvénic components, perhaps even with  $A_-^2/A_+^2 > 1$  in many of the cases with  $\rho P > 0$ . The important point is that although inwardly propagating Alfvén waves may at times occur, they evidently never occur in an extremely pure form, since  $|\rho| \geq .8$  implies  $\rho P < 0$ . Even though there may be periods in which there are both inward and outward Alfvén waves, there are no periods with exclusively inward propagation, whereas periods with exclusively outward propagation evidently occur on the order of 30 percent of the time.

It is clear from Table 1 that Alfvén waves propagating outward have a strong influence on the sign of  $\rho$ , even down to  $|\rho| = .4$ . This close correspondence between the sign of  $\rho$  and the polarity, together with the high percentage of times with  $|\rho| \geq .6$ , strongly indicates that outwardly propagating Alfvén waves dominate the microscale structure about 50 percent of the time. Coleman [1967] found precisely the same type of correlation shown in Table 1 in a study of cross spectra between plasma and magnetic field data from Mariner II (Venus 1962), and also noted that this type of correspondence between  $\rho$  and  $P$  would be expected for outwardly propagating Alfvén waves. The waves were thus also present in appreciable quantities in the interplanetary medium in 1962.

## Patterns of Occurrence

As noted above, Alfvén waves in the interplanetary medium have characteristic patterns of association with the large scale velocity structure of the solar wind. The macroscale properties of this stream structure were first discovered in the Mariner II data [Neugebauer and Snyder, 1966; Snyder et al., 1963], and subsequent probes have confirmed these initial results [Wilcox and Ness, 1965]. Although the high velocity streams observed by Mariner V are not as long lived as those found previously, the streaming patterns in the Mariner V data are very similar to those observed by earlier spacecraft, and exhibit the basic characteristics of fast and slow streams and their interactions. Figure 3 is a plot of three hour averages of various quantities over a 35 day period of the flight;  $V_w$  is the wind velocity,  $B$  is the magnetic field,  $N$  is the proton number density, and  $V_T$  is the most probable proton thermal velocity  $(2kT_p/m_p)^{1/2}$ . High velocity regions in the solar wind tend to be hotter and less dense and low velocity regions colder and more dense. The level of high frequency magnetic field activity also tends to be higher in high velocity streams, although this effect is not as pronounced as the correlation between velocity and temperature. Magnetic field strengths tend to be the same in both high and low velocity regions, except for the high field regions found at the leading edges of fast streams where the velocity increases rapidly with time. In these regions, high velocity streams are overtaking and colliding with low velocity ones, causing local compression and consequent high magnetic fields and densities; there are usually enhanced temperatures and very high levels of magnetic field activity in these colliding stream regions [Davis et al., 1966; Davis, 1966]. The best examples (as in Figure 1) of the purely Alfvénic, outwardly

propagating magnetic field fluctuations are found in high velocity streams and on their trailing edges (where the velocity decreases slowly with time). Regions with waves of this nature are indicated by the light bars in Figure 3. Alfvén waves found in low velocity streams are also outwardly propagating, but tend to be of lower amplitude than those in the fast streams, and tend to be less pure in the sense that they are more strongly intermixed with structures of definitely non-Alfvénic character (such as tangential discontinuities). The largest amplitude Alfvénic fluctuations are found in the colliding stream regions. However, waves in these regions may have significant amounts of inwardly propagating or non-Alfvénic components. Regions with very large amplitude waves are indicated by the heavy bars in Figure 3.

Figure 4 is a detailed specific example of large scale streaming properties using 40.3 minute averages plotted over a seven day period from day 189 to 195.  $\sigma_S$  is the square root of the 40.3 minute average of the total variance in the magnetic field components, in gamma, where the variances are computed over the plasma probe sampling period of 5.04 minutes, and the total variance is the sum of the variances on the individual axes. Gaps in the curves occur during periods when data were not taken. The region of rapid velocity increase at the leading edge of the high velocity stream extends from approximately the beginning to the end of day 192. It is preceded by relatively high densities, and is accompanied by enhanced temperatures and magnetic field fluctuations. The proton temperature and the standard deviations in field components are low in the low velocity stream, are at a maximum in the region of rapid velocity increase, and decrease with velocity on the trailing edge of the stream.

The proton number density falls to very low values inside the high velocity stream proper (on day 193, for example) as compared to values in the low velocity stream (day 189). The density increase from day 189 to the end of day 190 is probably not associated with the compression or pile-up of ambient slow gas ahead of the high velocity stream, since it is not accompanied by a field strength increase. The density increase is more likely a reflection of the observed fact that lower velocity streams have higher densities (note that the velocity is decreasing during this period). The density increase at the end of day 191 is accompanied by high field strengths, and thus is probably associated with compression of the slow gas ahead of the fast stream. The relatively higher field strengths and densities in the latter half of day 192 (as compared with day 193) are similarly the probable result of the deceleration and compression of the fast gas as it runs into the more dense slow gas. (Day 192, hours 15 to 18, has an average density and field strength of  $2.6 \text{ cm}^{-3}$  and 12.9 gamma, respectively, as opposed to average values of  $1.3 \text{ cm}^{-3}$  and 5.9 gamma on day 193, hours 0 to 3; although the field strength decrease in Figure 4 in the latter part of day 192 appears much larger than the density decrease, the relative change in the two quantities is the same.) In a later section we discuss further the dynamics of colliding stream structures.

Consider now the microscale fluctuations during this period. Their general level is indicated by the values of  $\sigma_S$  in Figure 4; their character is indicated by comparisons of  $\chi$  and  $b$  similar to Figure 1. These are shown for the most interesting part of the interval in Figure 5, in which lower frequency variations have been eliminated from all but the lower curve by subtracting from each point a smoothed low frequency mean

obtained by averaging over two hours about the point. The upper curves are thus high frequency variations about running two hour means. We emphasize that the vector velocity data given here are preliminary, and we present them only to demonstrate qualitative behavior. The variations in velocity have been multiplied by  $(4\pi \langle N \rangle m_p)^{1/2}$  (see equation (1)), where  $\langle N \rangle$  is the smoothed proton number density for each point, in order to normalize them to the magnetic field variations.  $B$  is the magnitude of the average magnetic field before low frequency averages are subtracted. Days 189 through 191 are very quiet magnetically, with little wave-like fluctuations at high frequencies; however, after the beginning of day 192 there is a high level of wave activity that is seen in Figure 5 to become obviously Alfvénic with good correlations on all three axes after hour 15. The correlation between  $\tilde{b}$  and  $\tilde{y}$  is particularly impressive in view of the fact that the plasma data is almost certainly highly aliased (changes in the plasma properties during the measurement of the energy spectrum) as there is a large amount of variation in the magnetic field with periods of less than five minutes, the plasma sampling period. For comparison Figure 6 is a point plot of 168.75 sec. averages of the magnetic field during days 192 and 193, showing more clearly the large amount of scatter in the field readings. The magnetic field variations in the compression region (before hour 21 in Figure 6) cannot be purely Alfvénic, since there are comparatively large fluctuations in  $B$  at higher frequencies. Even so, the power in the field magnitude at higher frequencies is small compared to the power in the field components, and the Alfvén mode is obviously still the dominant one. The polarity during this period is negative, and thus the very large amplitude higher frequency fluctuations (periods less than 2 hours) in the interaction region after hour 15 of day 192 are predominantly

propagating outward. Before hour 15, in the most active part of the compression region, the correlations are clearly not as good; this could be caused either by highly aliased plasma data, or by inwardly propagating Alfvénic or magnetoacoustic wave modes. On days 193 and 194, the amplitude of the field fluctuations has decreased (this period is in the high velocity stream proper), and the correlation between  $b_z$  and  $y$  is extremely good (as in Figure 1). The strength of the magnetic field fluctuations increases on all three axes as we move from the high velocity stream proper into the compression region at its leading edge; note, however, that the normal component of the field has more power than the radial or the tangential in the compression region itself (see Figure 6). This behavior appears to be a general property of field fluctuations in colliding stream regions.

Other examples of stream structure in the solar wind have characteristics similar to the above. Figure 7 is a plot of days 233 through 239 in the same format as Figure 4, except that now  $\sigma_S$  is the square root of the average total variance of the field components over 20.16 minute intervals (the plasma sampling period at the low data rate used here). In this example, the leading edge of the high velocity stream beginning on day 236 is preceded by dense low velocity gas and the trailing edge of another high velocity stream. Again we point out that the density increase across days 234 and 235 is almost certainly not associated with the pile-up of low velocity gas ahead of the high velocity stream, but instead is simply a reflection of the fact that lower velocities are associated with higher densities in the solar wind. This association is presumably because of conditions in the corona and the radial distribution of the energy supply of the solar wind. The increase in density and field strength from the beginning to the middle of day 236 is probably the result of a dynamic

compression of slow stream gas ahead of the fast stream, and the increase in field strength and density in going from day 237 to the last half of day 236 is probably due to the deceleration and compression of the fast gas as it runs into the slower, more dense gas ahead. Days 233 and 237 through 239 contain excellent examples of the pure outwardly propagating Alfvén wave mode. Days 234, 235, and the first half of 236 contain Alfvén waves, but they are intermixed with more slowly varying structures which are associated with changes in density and field strength, and which may be static (note the large changes in field strength and density on these two and a half days in Figure 7 as compared to the four days mentioned above). The last half of day 236 (the compressed fast gas) contains very large amplitude fluctuations which are primarily Alfvénic. Figure 8 is a high time resolution plot of the field variations in this period, showing in detail the enhanced field fluctuations in the compression region. The normal component of the magnetic field has more power than the other components in the latter half of day 236.

Figure 9 is a third example of large scale stream structure although in this case the situation ahead of the fast stream is somewhat chaotic. Day 285 after hour 6, and day 286 through the middle of day 287 contain good examples of purely Alfvénic, outwardly propagating waves. Days 282 through 284 contain outwardly propagating Alfvén waves of smaller amplitude, but these are strongly intermixed with large scale changes in field strength and density which may be tangential discontinuities or weak shocks. Figure 10 shows the change in the microscale fluctuations in the high velocity stream proper as they are swept into the compression region at the leading edge of the stream. Running backward in spacecraft time at hour 4 of day 285, one goes from unmodified high velocity gas to more disturbed gas that has already entered the compression region. The amplitude of the fluctuations increases, and again the normal component of the field variations is stronger. Figure 11 is another example

of large scale stream structure, and Figure 12 illustrates the character of the microscale magnetic field fluctuations in three distinct regions: the low velocity stream proper (day 227), the compressed leading edge of the high velocity stream (day 228), and the high velocity stream proper (day 231). Day 227 has some high frequency Alfvénic activity intermixed with large scale static structures, day 228 has very large amplitude waves which are predominantly Alfvénic (and which have more power in the normal direction), and day 231 has good examples of outwardly propagating Alfvén waves. Figure 13 is a plot similar to Figure 5, and demonstrates that the fluctuations on days 231 and 232 are extremely pure, outwardly propagating Alfvén waves. The average correlation between  $B_R$  and  $v_R$  for the four six-hour periods of day 228 was .5 (as opposed to an average of .88 for day 231), and the high frequency variance in the field strength is relatively high (as compared with day 231), so that the waves on day 228 in the compression region cannot be said to be purely Alfvénic or outwardly propagating, although they appear to be predominantly so.

#### Correlations between Three Hour Parameters

The character of these general patterns in the stream structure of the solar wind can be seen in correlation coefficients computed between various three hour average parameters over a solar rotation. Correlation coefficients, means, and standard deviations have been calculated for each of the six rotations 1832 through 1837, and Table 2 gives the average of these quantities over the six rotations, weighted according to the number of three hour data in a rotation. The number of three hour data averages per solar rotation varied from 95 (1835) to 195 (1834), with an average of 160 per rotation.  $V_W$ ,  $N$ ,  $V_T$ , and  $B$  are as defined above, and  $\beta_p$  is

Table 2. Weighted averages of correlation coefficients computed over the six solar rotations of the Mariner V flight. AVE and STD are weighted averages of the average and standard deviation of the various parameters over a solar rotation.

	$V_W$	N	$V_T$	B	$\beta_p$	$ \rho $	$\sigma_{S1}$	$\sigma_{S2}$	$\sigma_{S3}$
$V_W$	1.00	-.51	.66	.16	-.10	.07	.44	.37	.23
N	-.51	1.00	-.36	.08	.31	-.14	-.02	.10	.24
$V_T$	.66	-.36	1.00	.22	.18	.03	.55	.48	.32
B	.16	.08	.22	1.00	-.52	-.06	.52	.55	.56
$\beta_p$	-.10	.31	.18	-.52	1.00	-.10	-.12	-.10	-.11
$ \rho $	.07	-.14	.03	-.06	-.10	1.00	.09	.06	.06
$\sigma_{S1}$	.44	-.02	.55	.52	-.12	.09	1.0	.93	.76
$\sigma_{S2}$	.37	.10	.48	.55	-.10	.06	.93	1.0	.87
$\sigma_{S3}$	.23	.24	.32	.56	-.11	.06	.76	.87	1.0
AVE	410.	8.5	42.8	8.5	.60	.63	1.46	2.68	4.23
STD	75.	5.4	14.8	3.0	.51	.27	.65	1.25	2.09

the ratio of a proton thermal energy density to magnetic field energy density ( $4\pi m_p N V_T^2 / B^2$ ) computed using the three hour averages of  $N$ ,  $V_T$ , and  $B$ ;  $|\rho|$  is the absolute value of the correlation coefficient  $\rho$  between  $B_R$  and  $V_R$  computed over three hour intervals.  $\sigma_{S1}$  and  $\sigma_{S2}$  are the square roots of the three hour average of the 168.75 sec and 22.5 minute total variances in field components, respectively;  $\sigma_{S3}$  is the square root of the three hour total variance in components. Thus  $\sigma_{S1}$  is representative of the amount of power in the very high frequency magnetic field fluctuations during each three hour interval;  $\sigma_{S2}$  and  $\sigma_{S3}$  are representative of the power at lower frequencies.

From Table 2 we see that  $V_W$  is well correlated both with  $V_T$  and with  $\sigma_{S1}$ . These high correlations occur because high velocity streams are generally hotter, with more power in high frequency field fluctuations. The good anti-correlation between  $V_W$  and  $N$  reflects the generally lower densities of higher velocity regions. The high correlation between  $V_T$  and  $\sigma_{S1}$  occurs both because each is higher in high velocity streams and because local "hot" spots in temperature are usually associated with stream-stream collision regions, which contain very large amounts of high frequency magnetic field fluctuation.  $B$  correlates well with  $\sigma_{S1}$  because  $B$  is generally high during the stream-stream collisions, where  $\sigma_{S1}$  is high. Note that even though  $B$  and  $\sigma_{S1}$  correlate well, and  $V_W$  and  $\sigma_{S1}$  also correlate well,  $B$  and  $V_W$  are poorly correlated; this comes about because both  $\sigma_{S1}$  and  $B$  are enhanced in the colliding stream regions (where  $V_W$  is low and increasing), whereas  $B$  falls off and  $\sigma_{S1}$  stays at relatively high values during the high velocity stream itself.

The standard deviations in field components characteristic of lower frequency variations ( $\sigma_{S2}$  and  $\sigma_{S3}$ ) are not as well correlated with  $V_T$  and  $V_W$  as is  $\sigma_{S1}$ . We ascribe this to the fact that  $\sigma_{S2}$  and  $\sigma_{S3}$  are more strongly influenced by the presence of long term trends and large scale, non-wavelike structures (such as polarity reversals, compression regions, tangential discontinuities, etc.). The parameter  $\sigma_{S1}$  is comparatively free of such low frequency effects, and we feel that it is the best index to the relative strength of the dynamic, wave-like fluctuations in the magnetic field.

There is a good anti-correlation of  $\beta_p$  with  $B$ , but poor correlations with  $N$  and  $V_T$ , even though these quantities are used in its computation; this indicates that the magnetic field strength is the dominant factor producing variation in  $\beta_p$ .  $\beta_p$  correlates very poorly with  $V_W$  and  $\sigma_{S1}$ . High velocity streams, even though they are hotter, are not necessarily high  $\beta_p$  regions, because in general the density is lower. Also, the interaction regions between high and low velocity streams (where  $\sigma_{S1}$  is highest) are not necessarily high  $\beta_p$  regions, even though these regions are local "hot" spots, because usually the magnetic field strength is also very high. In general,  $\beta_p$  is a very poor index for the strength of the high frequency magnetic field fluctuations, and thus we conclude that these fluctuations are not governed by the local balance between proton thermal energy density and magnetic field energy density (in contrast to the conclusions of Burlaga, Ogilvie and Fairfield, 1969). Rather the strength of the microscale fluctuations is predominantly governed by the non-local (i.e., macroscale) properties of the solar wind, such as stream structure and generation or amplification of waves in colliding stream regions, and the best index to the strength of these fluctuations is the proton temperature  $V_T$ .

Table 2 shows that  $|\rho|$ , which is an indication of the presence of the waves, correlates very poorly with all other quantities; this fact was the basis for the statement in Paper I that the Alfvén waves have "...no discernible pattern of association with large scale structures such as high velocity streams...". As far as the presence of the waves is concerned, this statement is strictly true; examples of the Alfvén waves can be found under almost any macroscale condition. However, although  $|\rho|$  is an index to the presence of the waves, it gives no indication as to their amplitudes, and this is the property of the waves which correlates with the macroscale velocity structure.

In summary, we find that Alfvén waves in the solar wind are quite common, and may occur under most conditions. The purest examples of the outwardly propagating Alfvénic fluctuations are found in high velocity streams and on their trailing edges. Outwardly propagating Alfvén waves are also found in low velocity regions, but they tend to be of smaller amplitude and less pure in the sense that they are more strongly intermixed with structures which are not wavelike and possibly static. The largest amplitude Alfvén waves in the solar wind are found in the compression regions at the leading edges of high velocity streams; these regions may have inwardly propagating or non-Alfvénic wave modes. This characterization of Alfvén wave properties as related to stream structure is a generalized description only and notable exceptions exist. The macroscale properties of stream structure can be quite different from the examples we have given (i.e., shocks, etc.), and very large amplitude Alfvén waves can be found away from colliding stream regions (and even in low velocity streams, for example). However, the pattern described above occurs repeatedly throughout the five months of data from Mariner V, and appears to be a basic property of stream structure in the interplanetary medium.

## Wave Spectra and Energy Densities

The frequency range over which the waves extend is extremely broad. Figure 14 is a plot of the cross spectrum between  $B_R$  and  $V_R$  for a two day period of good waves, computed with 30 degrees of freedom and giving estimates for coherency and phase at frequencies from  $1/(4.2 \text{ hours})$  up to the Nyquist frequency of  $1/(10.08 \text{ minutes})$ . High coherencies and  $0^\circ$  phase are indicative of the presence of the waves; they extend from a low frequency cutoff of about  $1/(2 \text{ hours})$  up to the highest frequency measurable by the plasma probe,  $1/(10.08 \text{ minutes})$ . Cross-spectra of other segments of the data when waves are present show the same qualitative behavior. Taking into account the convective motion of the wind, these frequencies correspond to waves in the rest frame of the wind with periods from roughly 80 minutes (or less) to 16 hours, and wavelengths from  $.25 \times 10^6 \text{ km}$  (or less) to  $5 \times 10^6 \text{ km}$ .

It is likely that velocity fluctuations are well correlated with the magnetic field fluctuations at much higher frequencies than we can experimentally measure ( $1/(10.08 \text{ min.})$ ). The velocity can easily follow the abrupt transitions shown in Figure 2, and the properties of the magnetic field fluctuations above frequencies of  $1/(10 \text{ min.})$  are similar to those below  $1/(10 \text{ min.})$  (as discussed in the next section). Hence the higher frequency fluctuations in periods of good Alfvén waves are probably also Alfvénic. Since there is some variation at even the highest measurable frequency (see Figure 2), we would argue that the Alfvén wave number spectrum typically extends from  $10^3 \text{ km}$  to  $5 \times 10^6 \text{ km}$ .

Preliminary power spectra and cross spectra of the interplanetary magnetic field in the frequency range from  $1/(107.5 \text{ min.})$  to  $1/(25.2 \text{ sec.})$  have been calculated over most of the high data rate part of the mission,

using the fast Fourier transform [Hinich and Clay, 1968]. Each spectra is computed with 32 degrees of freedom, using 4096 averages, each 12.6 seconds in length (~14.3 hours of data); the resulting power spectral estimates are displayed on log-log plots, assuming a frequency dependence of  $f^{-\alpha}$ . The power levels obtained agree with those of earlier studies [Siscoe, et al, 1968; Coleman, 1966], except for those of Sari and Ness [1969], whose estimates during days of comparable magnetic field activity are in error by a factor of 10 to 100. In the range from approximately 1/(10 min.) to 1/(25.2 sec.), the spectra quite generally exhibit values of  $\alpha$  close to 1.6 or 1.7; in the range from 1/(107.5 min.) to 1/(10 min.), there is a much broader spread in values of  $\alpha$ , from as low as 1.5 to as high as 2.2. There is some indication that high values of  $\alpha$  ( $\alpha \approx 2.$ ) in this frequency range are associated with cold plasma regions, where there is little high frequency field fluctuation, and that low values of  $\alpha$  ( $\alpha \approx 1.5$ ) are associated with hot plasma regions, where there is a high level of high frequency field fluctuation (Table 2). A detailed study of least squares fits of  $\alpha$  as a function of various plasma parameters is being made to test such possible correlations.

Slopes of spectra during periods of very good waves (high correlation, little variance in field strength and density) tend to cluster about 1.7, but can be as high as 2. in the low frequency range mentioned above. It should be noted that an  $f^{-2}$  spectral dependence is completely consistent with the observed properties of the waves; such a spectrum can result both from a succession of discontinuities [Siscoe, et al 1968] or from irregular waveforms having no discontinuities. As we have seen, the waves can appear either as very irregular with gradual changes or as discontinuous, both on the time scale of Figure 1 and at the highest time resolution

(Figure 2 and Figure 16). In contrast to Sari and Ness [1969], we strongly support the conclusions of Coleman [1967] that the observed fluctuations of the interplanetary magnetic field as measured by power spectra and especially as correlated with plasma measurements, indicates the existence of waves in the interplanetary medium.

When the waves are prominent, the energy densities associated with them are comparable to magnetic field and kinetic energy densities [Coleman, 1967, 1968]. For various three hour intervals which are dominated by wave activity we take the total wave energy density  $W_E$  to be half magnetic and half kinetic energy of plasma motion, and to be equal to  $\delta B^2/4\pi$ , where  $\delta B^2$  is the total variance in field components over the three hour period. We compare this quantity to  $B^2/8\pi$  and  $NKT_p$  in Table 3. The three regions designated as periods of extreme field activity are all located at the leading edges of high velocity streams; those designated as moderate to quiet occur in the main bodies of streams or on their trailing edges. In all of these regions,  $W_E$  is comparable to field or thermal energy densities.

#### Anisotropy in the Microscale Fluctuations

In the previous section dealing with the wave spectra, we made no reference to or use of the vector nature of the magnetic field fluctuations. Power levels and slopes were estimated on the basis of spectra computed on each of the three RTN cartesian axes, treating variations in each direction as independent variables and neglecting their vector properties. We now consider directions of maximum and minimum power in a preferred coordinate system, using a method employed by Sonnerup and Cahill [1967] and by Siscoe et al. [1968] which allows one to deduce power levels along any given

TABLE 3

Period	$8\pi W_E/B^2$	$W_E/NKT_p$	Field Activity
167 12/15	.53	.95	moderate
192 15/18	.42	.88	extreme
195 12/15	.05	.13	quiet
228 12/15	.64	2.67	extreme
231 12/15	1.27	1.45	moderate
236 15/18	.42	1.28	extreme

direction. We first discuss the general properties of the microscale variations in magnetic field, and then examine in detail specific periods of dynamical interest.

The variance tensor  $\underline{S}$  is defined by  $S_{ij} = \langle B_i B_j \rangle - \langle B_i \rangle \langle B_j \rangle$ , where  $i, j$  refer to the RTN components of the magnetic field  $\underline{B}$ , and  $\langle \rangle$  denotes averaging over a specified time interval. The tensor components in any other system are given by the usual tensor transformation for rotation of axes. The trace of  $\underline{S}$  is  $\sigma_S^2$  as defined above; it is invariant to rotation of axes and is the sum of the eigenvalues of the matrix. If  $\langle \underline{B} \rangle$  is the average field, then

$$\sigma_{\parallel}^2 = \sum \langle B_i \rangle S_{ij} \langle B_j \rangle / |\langle \underline{B} \rangle|^2$$

$$\sigma_{\perp}^2 = \sigma_S^2 - \sigma_{\parallel}^2$$

are the variances in the field parallel and perpendicular, respectively, to the average field direction. Hence they measure, respectively, the fluctuations that primarily change the field strength and those that primarily change the field direction.

The matrix  $\underline{S}$  can be diagonalized, yielding the eigenvalues  $P_1 > P_2 > P_3$ , and the corresponding eigenvectors  $\underline{S}_1, \underline{S}_2$ , and  $\underline{S}_3$ . The eigenvectors form the principle axes of the "variance" ellipsoid;  $\underline{S}_1$  is the direction of maximum variation and  $\underline{S}_3$  is the direction of minimum variation. The relative magnitudes of the eigenvalues provide information about the anisotropy that is independent of coordinate system used. For example, if  $P_1, P_2$ , and  $P_3$  are of approximately equal magnitudes, the fluctuations are approximately isotropic in three dimensions and the directions of the eigenvectors have little significance. If  $P_1$  and  $P_2$  are of comparable magnitude and much

larger than  $P_3$ , the fluctuations are isotropic in the plane whose normal is  $\underline{S}_3$ . If  $P_1$  is much larger than  $P_2$  or  $P_3$ , the fluctuations are primarily in the direction  $\underline{S}_1$ . In the Mariner V data, we characteristically see large fluctuations in field components with little change in field strength. For variations of this nature, we should expect  $\underline{S}_1$  and  $\underline{S}_2$  to be perpendicular to  $\langle \underline{B} \rangle$ , and  $\underline{S}_3$  to be parallel to  $\langle \underline{B} \rangle$ .

In order to study the general nature of the field variations using this formalism, we have calculated variance matrices and the corresponding eigenvalues and eigenvectors from the basic magnetometer data for the entire Mariner V mission. Three different averaging times have been used in computing the  $\underline{S}$  matrices -- 168.75 sec ( $2^{-9}$  day), 22.5 min ( $2^{-6}$  day), and 3 hrs. ( $2^{-3}$  day). Each period is longer than the preceding by a factor of eight. The properties of the 168.75 second variance matrices are characteristic of very high frequency fluctuations, whereas the 3 hour variance matrices provide information about much lower frequency variations. Of course, we include the effects of the higher frequency fluctuations in the calculation of 3 hour variances, but since the spectrum of the magnetic fluctuations obeys a power law, we expect the lower frequencies to dominate in any given period. For each of these intervals we have also calculated  $B$ , the average magnitude of the field, and  $P_4$ , the variance in the field strength. Table 4 then gives averages over the entire mission of various quantities based on these interval averages. No attempt has been made to separate dynamic from static (purely convected) structures -- all data has been included. The low average values of  $P_2/P_1$  and  $P_3/P_2$  imply that in general the eigenvectors  $\underline{S}_1$ ,  $\underline{S}_2$  and  $\underline{S}_3$  are well defined directions, and thus a study of their directional distributions is meaningful and of some interest.

The RTN system is a poor one in which to study the eigenvectors, since  $\langle \underline{B} \rangle$  is obviously a preferred direction (values of  $P_4/P_1$  are very small).

TABLE 4 Average Eigenvalue Properties

Averaging Period	No. of Matrices	$\langle P_1 \rangle$	$\langle P_2/P_1 \rangle$	$\langle P_3/P_2 \rangle$	$\langle P_3/P_1 \rangle$	$\langle P_4/P_1 \rangle$	$\langle P_1/B^2 \rangle$
168.75 sec	59488	2.3	.28	.30	.08	.16	.04
22.5 min	7523	7.4	.28	.32	.08	.10	.13
3 hr	990	16.8	.35	.37	.12	.08	.31

Since the flow direction of the solar wind also has physical significance and is approximately along  $\underline{e}_R$ , we resolve the eigenvectors from each interval in a field-velocity coordinate system shown in Figure 15 and defined as follows: Z is the direction of  $\underline{e}_B$ , the unit vector parallel to  $\langle \underline{B} \rangle$  for that interval, X is the direction of  $\underline{e}_B \times \underline{e}_R$ , and Y is in the direction  $\underline{e}_Z \times \underline{e}_X$ . Thus, fluctuations along X are perpendicular both to the average field for that interval and the radial direction. Note that the field-velocity coordinate system changes from interval to interval, since the direction  $\langle \underline{B} \rangle$  changes. For long averaging times,  $\langle \underline{B} \rangle$  tends to be along the spiral field direction and in the solar equatorial plane, and hence X tends to be along the N direction. For shorter averaging times, however,  $\langle \underline{B} \rangle$  frequently has a significant component out of the equatorial plane, and X no longer bears as close a relationship to the N direction. The ultimate justification for the use of these coordinate axes is that eigenvector distributions are symmetric in this system.

Table 5 gives the directional distributions in the field-velocity system of the eigenvectors associated with the 22.5 min. variance matrices; distributions for the 168.75 sec. and 3 hour matrices are similar. Directions are specified by the usual spherical polar coordinates  $\theta$  and  $\phi$ , where  $\theta$  is the polar angle from the Z-axis and  $\phi$  is an azimuthal angle measured from the X-axis. The range of  $\theta$  is divided into equal increments of  $\cos\theta$  to correct for solid angle effects. Thus the various bins in the distribution tables represent equal solid angles on the unit sphere, and a spatially isotropic distribution of vectors would have equal percentages in each bin. The full distribution in all eight octants of the unit sphere is not given for the following reasons: 1) the eigenvectors are arbitrary to a factor of  $\pm 1$ , so that we may give all vectors positive components along Z;

TABLE 5 Eigenvector Distributions 22.5 minute intervals

		$\tilde{S}_1$ : Direction of Maximum Variation					
		$\varphi$					
		0/18	18/36	36/54	54/72	72/90	0 to 90
$\theta$	0/41	.6	.6	.5	.4	.4	2.5
	41/60	1.1	1.1	1.0	1.0	.5	4.7
	60/76	3.8	3.8	3.3	2.4	1.6	14.9
	76/90	22.5	19.6	16.7	11.1	8.2	78.1
	0 to 90	28.0	25.1	21.5	14.9	10.7	
		$\tilde{S}_2$ : Direction of Intermediate Variation					
		$\varphi$					
		0/18	18/36	36/54	54/72	72/90	0 to 90
$\theta$	0/41	2.5	2.9	2.8	2.8	3.1	14.1
	41/60	1.5	1.9	2.3	2.3	2.5	10.5
	60/76	1.8	2.6	3.8	4.1	4.8	17.1
	76/90	7.5	9.2	12.1	14.3	15.3	58.4
	0 to 90	13.3	16.6	21.0	23.5	25.7	
		$\tilde{S}_3$ : Direction of Minimum Variation					
		$\varphi$					
		0/18	18/36	36/54	54/72	72/90	0 to 90
$\theta$	0/41	12.0	13.5	14.6	17.4	19.4	76.9
	41/60	.7	1.1	1.3	2.3	2.4	7.8
	60/76	.4	.7	1.4	1.7	1.9	6.1
	76/90	.6	1.4	2.0	2.5	2.7	9.2
	0 to 90	13.7	16.7	19.3	23.9	26.4	

2) examination of the distributions thus obtained reveals that they are symmetric both about the XZ plane and the YZ plane. Thus by reflection in these two planes we obtain a representative distribution in the first octant only; distributions in other octants are symmetric reflections of the first octant.

The distributions presented demonstrate that  $\underline{S}_3$  has a strong tendency to be parallel to  $\langle \underline{B} \rangle$  ( $\theta = 0^\circ$ ), whereas  $\underline{S}_1$  and  $\underline{S}_2$  are generally perpendicular to  $\langle \underline{B} \rangle$  ( $\theta = 90^\circ$ ) as we would expect. In addition,  $\underline{S}_1$  tends to be nearer the X-axis ( $\varphi = 0^\circ$ ) than the Y-axis ( $\varphi = 90^\circ$ ); i.e., the direction of maximum power tends to be in the  $\underline{e}_B \times \underline{e}_R$  direction. This is true for each of the three different averaging times, and thus is characteristic of the microscale fluctuations over a broad frequency range. It should be remembered that the higher frequency fluctuations are superimposed on lower frequency fluctuations with larger amplitudes. The higher frequency fluctuations hence appear to adjust themselves to the average "background" field that they see, even though this field is changing as part of a lower frequency variation.

Having established that this non-stationary field-velocity coordinate system is preferred for the microscale fluctuations, we compute variances of the field along the XYZ axes. The variance of the magnetic field in a direction  $\underline{e}_D$  is given by  $\underline{e}_D \cdot \underline{S} \cdot \underline{e}_D$ , where  $\underline{S}$  is the variance matrix. Table 6 gives the average fractional variances for both the XYZ and the RTN systems;  $P_S = P_X + P_Y + P_Z = \text{Trace}(\underline{S})$  and is thus independent of any particular coordinate system.  $\langle \rangle$  denotes long term averages of the properties of variance matrices for a given time interval; in Table 6 the averages are taken over the entire Mariner V mission. In the XYZ system,  $\langle P_X/P_S \rangle$ , the average fractional variance in the X direction, is consistently larger

TABLE 6 Average Fractional Variances

Averaging Period	No. of Matrices	$\langle P_S \rangle$ $\gamma^2$	$\langle P_X/P_S \rangle$	$\langle P_Y/P_S \rangle$	$\langle P_Z/P_S \rangle$	$\langle P_R/P_S \rangle$	$\langle P_T/P_S \rangle$	$\langle P_N/P_S \rangle$
168.75 sec	59488	2.6	.51	.38	.11	.26	.33	.40
22.5 min	7523	9.3	.52	.37	.11	.25	.34	.41
3 hr	990	23.8	.47	.36	.17	.26	.34	.40

than  $\langle P_Y/P_S \rangle$ , which is in turn larger than  $\langle P_Z/P_S \rangle$ , as we would expect from the eigenvector distributions. In the RTN system,  $\langle P_N/P_S \rangle$  is larger than  $\langle P_T/P_S \rangle$  and  $\langle P_R/P_S \rangle$  for all averaging times, as we would expect from the orientation of the XYZ system with respect to the RTN system. The  $\underline{e}_B \times \underline{e}_R$  direction is of more significance than the  $\underline{e}_N$  direction, as is shown by the fact that  $\langle P_X/P_S \rangle$  is 25% larger than  $\langle P_N/P_S \rangle$ . We note that R and T do not display equal amounts of power (as we might naively assume from the average orientation of the XYZ system) because the direction of maximum power,  $(\underline{e}_B \times \underline{e}_R)$ , is always perpendicular to the R direction, whereas it can have a large component along the T direction if  $\underline{e}_B$  has a significant N component. Table 6 also indicates that the average fractional variance along the field direction is larger for the three hour intervals than for the 22.5 min. or 168.75 sec. intervals, even though Table 4 shows that the ratio of variance in field strength to the maximum component variance is smaller for the three hour intervals. These results at first appear inconsistent, but it must be remembered that for long averaging times the standard deviations in components become comparable to the background field strength (Table 4) and consequently the concept of an "average" background field direction is not as well defined for the three hour intervals in Table 6 as it is for the shorter averaging times. Thus we can characterize the general statistical nature of the micro-scale fluctuations as consisting primarily of variations perpendicular to the average field direction ("average" referring to the time scale of interest), with more power along the  $\underline{e}_B \times \underline{e}_R$  direction over a wide range of frequencies. In the RTN system these properties produce on the average more power in the N direction, with minimal power along the R direction.

For completeness, we mention that one can also apply the basic ideas used above in a more sophisticated power spectral analysis. For every six hour interval in the Mariner V mission with sufficient data return, we have computed auto and cross spectral estimates with 32 degrees of freedom, using 168.75 second averages of the magnetic field. This process yields (for each 6 hour interval) eight power spectral tensors (each with six independent elements, three auto powers and three cross powers) at eight uniformly spaced frequencies in the frequency range from  $1/(45 \text{ min})$  to  $1/(5.625 \text{ min})$ . These matrices were diagonalized to obtain characteristic directions of maximum and minimum power, etc., for each frequency; properties of the power matrices (for each individual frequency) averaged over the entire mission are similar to the properties of the variance matrices described above, over the entire frequency range. The advantage of the power spectral method lies in the fact that it can describe anisotropies characteristic of a specific frequency, whereas the variance matrix approach gives results that are in some sense representative of all frequencies above a certain minimum frequency. The drawback of the power spectral method is that it is difficult to define an average field direction for the higher frequency fluctuations, since they are superimposed on larger amplitude low frequency variations; thus, distributions similar to those in Table 5 for the higher frequency spectral estimates (using the 6 hour averaged magnetic field as the direction of  $\underline{e}_B$ ) are not as strongly peaked as those in Table 5. The variance matrix approach, on the other hand, provides an obvious and physically appropriate average "background" field for each interval, and hence provides the most sharply peaked distributions. In any event, the two methods give basically the same result, conclusively demonstrating that the anisotropies described above are characteristic of the microscale fluctuations over a wide frequency range.

In the above considerations we have made no attempt to select data on any basis; every interval of the Mariner V mission with sufficient data return has been included. If we compute distributions such as given in Tables 4 through 6 for individual solar rotations instead of for the entire mission (as above), we obtain essentially the same results except for the increase in power level ( $P_S$ ) as Mariner V approaches the sun. Average fractional variances and eigenvector distributions remain approximately the same from one solar rotation to the next, even though the average power level of the fluctuations increases, and it appears that the  $\epsilon_{B^2}^{\text{ex}} \epsilon_R$  fractional power excess averaged over a solar rotation is independent of distance from the sun in the range .7 to 1 a.u.

Since all data are included in these analyses, with no attempt to distinguish dynamic from static effects, the observed  $\epsilon_{B^2}^{\text{ex}} \epsilon_R$  anisotropy might be caused either by a dynamical process associated with fluctuations propagating in the rest frame of the wind, or, perhaps, by some preferred orientation of static irregularities convected by the solar wind. To resolve this ambiguity, we have computed distributions similar to those in Tables 4 through 6 for each day of the mission, using 22.5 minute variance matrices (64 per day) and 168.75 second variance matrices (512 per day). The 168.75 second variances invariably show values of  $\langle P_X/P_S \rangle$  (averaging over one day) larger than  $\langle P_Y/P_S \rangle$  or  $\langle P_Z/P_S \rangle$ . Only on very quiet days is  $\langle P_X/P_S \rangle$  approximately equal to  $\langle P_Y/P_S \rangle$ ; on more active days (moderate power at high frequencies) values for the different parameters averaged over the day are closely similar to those given in Table 6. The properties of the 22.5 minute variances, considered on a day to day basis, also exhibit the expected anisotropies, although not as consistently as do the 168.75 second variances (139 days out of 150 have  $\langle P_X/P_S \rangle > \langle P_Y/P_S \rangle$ ). More

significantly, the  $e_{\underline{B}} \times e_{\underline{R}}$  anisotropy tends to be most pronounced in the interaction regions between high and low velocity streams, for both averaging times. For example, Table 7 gives the distribution of eigenvectors associated with maximum variation for both 168.75 second and 22.5 minute intervals on day 192. As previously mentioned, this is a period of rapid velocity increase and large magnetic field variations (see Figure 4). Table 7 indicates that both the 22.5 minute and 168.75 second intervals have a strongly enhanced  $e_{\underline{B}} \times e_{\underline{R}}$  anisotropy as compared to the average values (Tables 4 through 6). Figure 6 is a point plot of 168.75 second field averages on this day, clearly showing larger fluctuations in the normal component of the field at low frequencies. Figure 16 is a plot of one hour of basic magnetometer data (one reading in approximately 4 seconds) on this same day, showing roughly the same effect at higher frequencies. On the following day (193) the wind velocity levels off and the power in the field fluctuations decreases (see Figure 6); the anisotropy in the 168.75 second variances decreases almost exactly to the values given in Table 6, and the  $e_{\underline{B}} \times e_{\underline{R}}$  anisotropy in the 22.5 minute variances essentially disappears. Figures 8 and 12 illustrate this same effect in the microscale fluctuations of day 228 and 236, which are the interaction regions for the streams shown in Figures 7 and 11. Since the most prominent  $e_{\underline{B}} \times e_{\underline{R}}$  anisotropies tend to occur during regions of definitely non-static character, it is clear that the effect is a dynamic one, and not due to some peculiar orientation of static, convected discontinuities. This is not meant to imply that the anisotropy occurs only in stream-stream interaction regions, as it is essentially always present at high frequencies, and usually present at lower frequencies.

TABLE 7

$S_1$  : Direction of Maximum Variation (168.75 sec intervals), Day 192

$\theta$	$\phi$					
	0/18	18/36	36/54	54/72	72/90	0 to 90
0/41	.0	.0	.0	.0	.0	.0
41/60	.0	.0	.0	.0	.0	.0
60/76	1.3	2.2	2.2	.3	.9	6.9
76/90	31.0	26.9	16.5	7.9	10.8	93.1
0 to 90	32.3	29.1	18.7	8.2	11.7	

168.75 sec, 316 matrices:

$$\langle P_S \rangle = 6.9\gamma^2, \quad \langle P_X/P_S \rangle = .59, \quad \langle P_Y/P_X \rangle = .36, \quad \langle P_Z/P_S \rangle = .05$$

$S_1$  : Direction of Maximum Variation (22.5 min intervals), Day 192

$\theta$	$\phi$					
	0/18	18/36	36/54	54/72	72/90	0 to 90
0/41	.0	.0	.0	.0	.0	.0
41/60	.0	2.5	.0	.0	.0	5.0
60/76	7.5	5.0	2.5	.0	2.5	17.5
76/90	35.0	17.5	12.5	7.5	5.0	77.5
0 to 90	42.5	25.0	15.0	7.5	7.5	

22.5 min, 40 matrices:

$$\langle P_S \rangle = 18.2\gamma^2, \quad \langle P_X/P_S \rangle = .60, \quad \langle P_Y/P_S \rangle = .30, \quad \langle P_Z/P_S \rangle = .10$$

## DISCUSSION

### Possible Origins

As we have seen, Alfvén waves occur quite often in the solar wind, and their energy densities are frequently comparable both to unperturbed magnetic fields energy densities and to thermal energy densities. The origins and energy sources for these waves are thus of considerable interest, as is their contribution to the dynamics and heating of the solar wind. We consider three possibilities: (1) the waves are produced locally in the solar wind (in the same general region where they are observed) by internal plasma instabilities; (2) the waves are produced locally by large scale velocity differences in the solar wind; (3) the waves are remnants of processes occurring in the solar photosphere, chromosphere, or corona. We discuss these points in some detail, especially as they relate to the heating of the solar wind by means other than thermal conduction.

(1) Parker [1963] has pointed out that local thermal anisotropies due to the radial expansion of the solar wind should lead to "internal" plasma instabilities and subsequent wave generation. It is not immediately apparent that waves generated by such instabilities would propagate predominantly outward along field lines, although such preferential generation might, for example, stem from the high energy tail of the thermal proton distribution (which is outward along field lines [Hundhausen et al., 1967]). However, plasma instabilities such as the firehose instability [Parker, 1963; Scarf, Wolfe, and Silva, 1967] do not efficiently generate waves with wavelengths many orders of magnitude longer than the ion cyclotron radius ( $\sim 100$  km). As the dominant wavelengths at issue are on the order of  $10^6$  km, with decreasing power at shorter wavelengths, it seems unlikely that internal plasma instabilities are of importance in their generation.

(2) Several models have been proposed in which large scale velocity differences in the solar wind provide the basic energy source for the microscale fluctuations. In the analysis of the Mariner II data, it was suggested [Neugebauer and Snyder, 1966; Davis, et al, 1966] that the heating and high magnetic field activity found in the compression regions at the leading edges of high velocity streams were generated locally by the faster streams overtaking and colliding with slower streams. Jokipii and Davis [1969] pointed out the importance of such stream-stream collisions as a source of wave and thermal energy in the solar wind. They noted that if the collisions are predominantly between clouds moving radially, the compression will be mainly in the radial direction, and this will produce more fluctuation in the transverse than the radial component of the magnetic field, in accord with observations (Table 6) [Coleman, 1966; Siscoe et al, 1968]. It seems quite plausible that the high level of magnetic field activity in colliding stream regions is freshly generated, but there is no obvious reason to expect waves produced in this manner to propagate predominantly outward in the rest frame of the wind.

The relatively smaller amplitude fluctuations away from such regions might also be related to this type of generation process, although there are major difficulties with this view. As Burlaga and Ogilvie [1970] point out, colliding stream regions occur infrequently and are of relatively limited spatial extent at 1 a.u. (cf. Figure 3). Alfvén waves generated in these regions cannot leave them faster than the Alfvén velocity, and hence can propagate at most of the order of .1 a.u. away from their point of generation by the time the solar wind reaches 1 a.u. As will be seen below, field lines tend to make a rather small angle with the interface between high and low velocity regions, and hence waves that propagate along field lines leave the interface at a normal velocity that is much less than the Alfvén

velocity. Thus Alfvén waves in the main body of a stream well away from regions of rapid velocity increase (greater than 12 hours away in the spacecraft frame) cannot be associated with waves generated in those regions. This is especially true of Alfvén waves in high velocity streams, since these waves are propagating toward the collision region rather than away from it. Observationally, the level of the field fluctuations usually drops abruptly immediately outside the colliding stream regions, as can be seen in Figures 6, 8, and 10, for example. It thus appears [Burlaga et al, 1970] that the large amplitude fluctuations found in the colliding stream regions cannot effectively propagate away from them.

It could be argued that fine scale velocity differences near the sun might produce waves but be completely eliminated by the time the solar wind has reached 1 a.u., leaving behind Alfvén waves and enhanced temperatures in the main body of the streams. It is unlikely, however, that such a process will have occurred on the trailing edges of the high velocity streams where the velocity is decreasing with time, even though we observe reasonably pure Alfvén waves in these regions. There is also no convincing reason to expect such collisions to generate Alfvén waves propagating exclusively outward in the rest frame of the wind. Thus although there is little question that stream-stream collisions are an important energy source for the large amplitude waves actually found in the colliding stream regions, it seems implausible that they are also responsible for the relatively smaller amplitude Alfvén waves found in the main body of velocity streams.

In a somewhat different approach that does not emphasize colliding stream regions, Coleman [1968] has proposed a turbulent model of the solar wind in which all large scale differential velocities feed energy into a hierarchy of turbulent eddies through instabilities associated with the

shear and compression of the plasma. The fluid is treated as uniformly turbulent with a non-linear cascade of energy through Alfvénic turbulence of intermediate wavelengths, where there is little dissipation, to very short wavelengths, where cyclotron damping converts the wave energy into thermal energy. As above, the major objection to such a model is the lack of an explanation for the predominantly outward propagation of the observed fluctuations. Also, in a collisionless magnetized plasma, the coupling between waves of different wave numbers seems likely to be quite different from that for the waves in fluids where conventional turbulence theory applies.

In summary, it appears that unless a plausible explanation for preferentially outward wave generation is advanced (and this seems unlikely), large scale velocity differences in the solar wind cannot be considered a primary energy source for the Alfvén waves observed at 1 a.u. However, such velocity differences in the solar wind streams do represent a potentially major source of energy for the microscale fluctuations, and may eventually become the dominant energy source beyond 1 a.u.

(3) It is commonly accepted that the solar corona is heated by the dissipation of magnetoacoustic wave energy generated at the photosphere [Van de Hulst, 1953]. Estimates of the energy requirements for heating the solar chromosphere and lower corona are  $5 \times 10^{29}$  ergs/sec and  $5 \times 10^{27}$  ergs/sec, respectively [Osterbrook, 1961]. The Alfvén waves observed at 1 a.u. represent a net outward efflux of energy on the order of  $3 \times 10^{24}$  ergs/sec, and can reasonably be viewed as the undamped remnants of waves produced at or near the sun. Recent theoretical work [Barnes, 1966] indicates that linear magnetoacoustic MHD waves are strongly damped in collisionless plasmas such as the solar wind (moderate to high  $\beta$ ), and that the Alfvén mode is undamped. Thus, by the time the solar wind

reaches .7 to 1 a.u. we would expect to observe only the Alfvénic remnants of what is perhaps a much broader spectrum of MHD waves generated closer to the sun. As long as the waves are produced at distances from the sun of less than Alfvénic critical point (15 - 50  $R_{\odot}$ ) [Weber and Davis, 1967], only those Alfvén waves propagating away from the sun will eventually appear in the superalfvénic solar wind. Generation of the observed Alfvén waves inside the Alfvénic critical point thus easily accounts for their preferential direction of propagation in the interplanetary medium. The waves can easily survive until they reach 1 a.u. since they are convected about ten times as fast as they propagate and hence make only on the order of  $1 \text{ a.u.} / 10\lambda$  oscillations for a wavelength of  $\lambda$ . For a wave of wavelength .01 a.u. this is only 10 oscillations.

The hypothesis that the interplanetary Alfvén waves are the remnants of "noise" introduced into the solar corona near the sun is an interesting one, since it suggests the possibility of monitoring small-scale solar activity from the orbit of the earth [Parker, 1965]. This possibility has important implications with regard to current theories of the heating of the solar wind by mechanisms other than thermal conduction. It is generally agreed that the solar wind requires an extended heat source above the base of the corona; if the only energy transport from the base of the corona is conduction and convection, the calculated density at the orbit of the earth in the two fluid model is too high, and both the velocity and proton temperature too low, as compared with observations [Sturrock and Hartle, 1966]. It has been suggested [Parker, 1969] that the energy equation of the solar wind is dominated near the sun by the transport and deposition of energy by waves. Barnes [1968, 1969] has proposed a model of solar wind proton heating by eventual dissipation of MHD waves generated at less than

1.5  $R_{\odot}$ , and Hartle and Barnes [1970] have shown that a heat source for protons added to the two fluid solar wind model can increase both the proton temperature and the wind speed and lower the density at 1 a.u. if the energy disposition takes place over an extended range ( $2R_{\odot} \leq r \leq 25 R_{\odot}$ ). In this model, more active regions of the sun with a higher level of wave generation could cause extensive heating of the corona by wave damping near the sun, thus producing solar wind streams with higher velocities and proton temperatures and lower densities as compared to streams without such heating. The higher level of pure, outwardly propagating Alfvénic wave energy observed in the high velocity streams can easily be interpreted as a signature of this process, since the purely outwardly propagating waves in the main body of the streams are very probably a direct consequence of "turbulent" conditions near the sun. The observational fact that the largest amplitude waves occur at the leading edges of the high velocity streams where the velocity is increasing rapidly (but before it is at a maximum) at first seems inconsistent with this model, since we would naively expect the highest wave amplitudes to be associated with the highest velocities. However, local wave generation and amplification due to compression at the leading edges of the high velocity streams can account for this, as we shall see in the next section. It seems most probable that the exclusively outwardly propagating Alfvén waves found in the main bodies of solar wind streams, away from sharp velocity changes, are generated in the vicinity of the sun. Alfvén waves which cannot be definitely said to propagate exclusively outward, such as those found in colliding stream regions, may be generated locally to a large extent.

### Quasi-Stationary Stream Structure in the Solar Wind

On the basis of the discussion in points (2) and (3) above, and taking into account observed patterns in the solar wind stream structure, we would like to suggest a qualitative model for the observed properties of the interplanetary Alfvén waves and their relation to the large scale structure of the interplanetary medium. First, we interpret the presence of high velocity, high proton temperature, low density streams in the solar wind as a probable result of extensive proton heating by wave damping near the sun; streams in which there has been a smaller amount of such heating have lower velocities and proton temperatures, higher densities, and less easily detectable Alfvén waves. The occurrence of larger amplitude, purely outwardly propagating Alfvén waves in the main bodies of the high velocity streams is presumed to be a consequence of this heating process. The streaming pattern of a non-rotating sun would be quite simple, consisting of a number of (non-circular) cones containing high velocity, low density, hot gas (with a high level of outward Alfvén wave activity) separated by low velocity, low temperature, dense gas (with a lower level of Alfvén wave activity). The rotation of the sun complicates this picture considerably. Solar rotation causes slow gas to be followed by fast, and fast by slow on the same radial line. The fast streams overtake the slow streams ahead, causing compression, and draw away from the slower streams behind, causing rarefaction.

Figure 17 illustrates what we consider to be the major features of the interaction between high and low velocity streams, assuming that the structures are long lived enough to be considered as quasi-stationary and corotating. The labeled regions in the upper half of Figure 17 have different physical characteristics. In the older, conventional double shock models [Dessler and Fejer, 1963; Davis, 1966] they would be separated

by shocks or contact surfaces; for the present discussion it does not matter whether the lines in the figure represent discontinuities, extended collisionless shock structures, or more or less continuous transition zones. Region S is the unperturbed slow stream and region F the fast stream followed by another slow stream. Region S' is the slow stream gas compressed and accelerated by the collision and region F' is the compressed and decelerated fast stream gas. The velocity vectors shown are those in an inertial frame; in this frame, the figure rotates with the sun.

It is instructive to consider this steady state flow in a rotating coordinate system. The structure in the upper half of Figure 17 now does not rotate; instead, the spacecraft moves clockwise in a circle and makes observations which, when plotted as functions of time, yield the idealized curves shown in the bottom half of the figure. In this corotating frame, the velocity is everywhere parallel to the smoothed magnetic field lines, and hence the flow is in a spiral whose pitch changes as it passes into the regions of compression because of the pressure gradient (or discontinuity) across the transition. The deflection provides a natural explanation for the observations [Lazarus, 1970; Wolfe, 1970] that in a region such as S' the solar wind appears to come from east of the sun while in a region such as F' it appears to come from the west. This aspect of the model is very similar to that of Siscoe, Goldstein and Lazarus [1969] except that they do not emphasize the distinction between the compressed interaction regions and the remainder of the fast and slow streams.

The flow along the magnetic spirals is from F to F' and from S to S'. In each case, the gas is compressed in the transition, and in the simple double shock model both transitions are ordinary fast shocks while the S'F' interface is a tangential discontinuity. The F to F' shock appears

to be running backward toward the sun into a low density region, and hence is often called a reverse shock. Because of the compression, both primed regions will have higher temperatures, densities, and field strengths than do the adjacent unperturbed gases in their respective streams. Typically, the fast stream is decelerated more in going from F to F' than the slow stream is accelerated in going from S to S', since the slow stream is more dense.

Although the simplest theoretical model is that of the ideal double shock, the observations rarely if ever show the expected discontinuities in velocity, density, and magnetic field. Either this represents a thicker than expected shock structure or there are no shocks and instead a continuous transition produced by some as yet unexplained mechanism. In either case, the Rankine-Hugoniot conservation theorems must hold across the transition, and most of the results of the simple shock analysis should be good approximations. Ideally, S' and F' are separated by a tangential discontinuity which neither plasma nor field lines cross, and in practice this can often be recognized as an abrupt change in density, temperature, and wave amplitude (for example see Figure 7, day 236, hour 12). The fact that the larger amplitude Alfvén waves from the fast stream appear to be confined to the fast stream side of this boundary (cf. Figure 8) is a strong indication that the field lines do not cross the boundary between the fast and slow streams.

In region R of Figure 17 there should be a rarefaction, causing a relative decrease in density in the leading part of the slow and the trailing part of the fast stream. The net result of the compression and rarefaction is the production of an asymmetry in the shape of the streams, as indicated in the lower part of Figure 17, that increases with the distance from the sun. This asymmetry in the streaming patterns, as well as many other features

of the model, can be seen both in the observational data presented above (cf. Figures 3, 4, 7, 9, and 11) and in the earlier Mariner 2 data [Neugebauer and Snyder, 1966]. We emphasize that in this model the increased density usually observed ahead of fast streams (Regions S and S') is for the most part not the result of the pileup of ambient gas ahead of the fast stream. Rather, it is primarily due to the fact that the energy supply at the base of the solar wind for the slow gas which precedes the fast is such as to produce higher densities in the slow gas (as well as lower velocities and temperatures at 1 a.u.

Imp I data, organized by Wilcox and Ness [1965] on the basis of the magnetic sector structure, i.e., the magnetic polarity, rather than the stream structure, also exhibit patterns similar to the curves in the lower half of Figure 17. The two methods of analysis give similar results because, in the case of the Imp I data, polarity reversals occur near the center of the prominent low velocity regions and there is a strong tendency for each high velocity stream to occupy its own sector. At the times of Mariners 2 and 5 this was not the case, since two or more adjacent high velocity streams have the same magnetic polarity. In these cases analysis based on solar wind velocity characteristics gives clearer patterns than does the use of magnetic polarity. This is plausible since the variations in energy supply associated with velocity variations are likely to be more basic than are changes in magnetic polarity. An explanation is needed for the observation that reversals of polarity apparently occur predominantly in low velocity regions. Perhaps the magnetic configuration in the lower corona near polarity reversals affects the energy supply to the solar wind in such a way as to favor low velocities.

## Patterns in the Microscale Fluctuations

The effect on the microscale fluctuations of the compressed regions in this quasi-stationary large scale streaming structure will be both to amplify existing waves and to generate fresh waves locally. Large amplitude, outwardly propagating Alfvén waves in region F propagate and are convected into region F'. If the Alfvén waves are initially polarized in the  $\hat{e}_N$  direction, then they will remain purely Alfvénic as they are swept into F' since their magnetic field fluctuations remain perpendicular to the average field direction. If they are polarized in the solar equatorial plane, they will be partially converted into magnetoacoustic waves because of the abrupt turning of the field lines in this plane across the transition (see Figure 17).

In any case, the amplitude of the waves will increase across the transition because of the compression. In the colliding stream region on day 192 (Figure 4), for example, we see a considerable increase in the amplitude of the waves as the compression region is entered (around hour 21 in Figure 6), although they remain predominantly outwardly propagating across the transition (Figure 5). If the transition between F and F' is smooth compared to a wavelength, we would expect the waves convected into F' to still be outwardly propagating. If the transition is an ideal thin shock, an outwardly propagating wave will produce both outwardly and inwardly propagating waves as it passes the discontinuity. However, the latter wave remains in F' and is not reflected back into region F, as would be the case for a discontinuity in a non-streaming medium, since the streaming velocity in a system in which the interface is stationary is faster than the wave velocity on the F side of the interface. Thus the

waves cannot escape from  $F'$  to  $F$  and Alfvén waves cannot escape into  $S'$  because the field lines do not cross the tangential discontinuity at the interface. Leakage out of the region  $F'$  is perhaps possible only because of the finite dimensions of the region normal to the field lines or by the partial conversion of the Alfvén mode into the magnetoacoustic modes. Thus Alfvén waves from  $F$  will be swept into  $F'$ , amplified by compression, and channeled outward along the compressed leading edge of the high velocity stream. We should expect this same general effect for waves swept from  $S$  into  $S'$ , although it should not be as pronounced since the waves convected from  $S$  into  $S'$  are typically of smaller amplitude than those in  $F$ .

At each transition we expect that the collision will, in addition to amplifying the convected Alfvén waves, generate additional fluctuations. These will presumably be a mixture of Alfvén and magnetoacoustic modes propagating both inward and outward. Again, these freshly generated waves will be primarily confined to the colliding stream region. Thus the total wave structure in the colliding stream regions will consist of higher amplitude fluctuations which are not as purely Alfvénic or outwardly propagating as are waves in the neighboring regions.

It appears that all of the observed properties of waves in the solar wind follow naturally from this model. Most of the waves in the interplanetary medium are outwardly propagating Alfvén waves from near the sun, and are remnants of the processes that supply energy to drive the different solar wind streams. Higher velocity streams undergo the most extensive heating, and thus contain the best examples of such waves. Compression of these waves and fresh generation of new fluctuations in colliding stream regions account for the waves with the largest observed amplitudes.

## The Microscale Anisotropies

The analysis of the observational data has revealed a number of anisotropies in the microscale magnetic fluctuations whose physical basis we now consider. The main points to be explained are that the minimum component of the fluctuations is parallel to  $\underline{e}_B$ , the direction of the average magnetic field, and that the maximum component is in the  $\underline{e}_B \times \underline{e}_R$  direction, where  $\underline{e}_R$  may be regarded as the direction of the solar wind flow. The first of the anisotropies is explained by the predominantly Alfvénic nature of the fluctuations. Thus we wish to understand why the Alfvén waves dominate the magnetoacoustic modes, and why they are partially polarized in the  $\underline{e}_B \times \underline{e}_R$  direction. Such properties may be due either to the mechanisms which generate the waves or to decay mechanisms.

It is unlikely that Alfvén waves are dominant solely because the magnetoacoustic modes are not generated strongly. In colliding stream regions, for example, we expect to see all types of hydromagnetic waves produced, but the fluctuations are primarily Alfvénic (little variance in field strength compared to large variance in components). Even if Alfvén waves are preferentially generated, we would expect them to excite magnetoacoustic modes either because of non-linearities in the equations of motion or because of geometrical considerations (a pure Alfvén wave must extend to infinity in the plane of polarization). Thus the observations suggest that magnetoacoustic modes must be damped at a rate sufficient for their reasonably complete removal from waves convected from near the sun and for partial removal from more locally generated waves. Barnes [1966] has shown theoretically that linear magnetoacoustic MHD waves are strongly damped in collisionless plasmas of moderate to high  $\beta$  ( $\beta > .5$ ) and that the Alfvén

mode is undamped. Thus this theory both explains and is confirmed by the observations.

There appears to be no plausible anisotropy in the generation of the Alfvén waves which would favor the  $\underline{e}_{\underline{B}} \times \underline{e}_{\underline{R}}$  direction. Thus we examine mechanisms which couple the undamped Alfvén waves into the strongly damped magnetoacoustic modes. For example, consider the convection away from the sun of Alfvén waves which are initially unpolarized. Assume that the magnetic field fluctuations are isotropic in the plane perpendicular to an average magnetic field along the classic spiral. As the waves are convected outward, the rotation of the sun causes the average field to turn in the plane normal to  $\underline{e}_{\underline{N}}$  as the spiral is generated. The component of the Alfvén waves originally polarized along  $\underline{e}_{\underline{N}}$  is unaffected by this turning since it always remains normal to  $\underline{e}_{\underline{B}}$ ; however, the component originally along  $\underline{e}_{\underline{B}} \times \underline{e}_{\underline{N}}$  develops a component along  $\underline{B}$ , and hence is coupled into magnetoacoustic modes. Thus the gradual spiraling of the field combined with the damping of the magnetoacoustic modes converts an initially isotropic distribution of Alfvén waves into one having more power along  $\underline{e}_{\underline{N}}$ .

If the average magnetic field is not along the ideal spiral then the expansion of the solar wind in the direction normal to  $\underline{e}_{\underline{R}}$  as it flows outward will turn the field vector in a plane whose normal is  $\underline{e}_{\underline{B}} \times \underline{e}_{\underline{R}}$ . The mechanism just described then produces an anisotropy in the  $\underline{e}_{\underline{B}} \times \underline{e}_{\underline{R}}$  direction. The  $\underline{e}_{\underline{B}} \times \underline{e}_{\underline{R}}$  and the  $\underline{e}_{\underline{N}}$  directions are in general close to each other unless  $\underline{e}_{\underline{B}}$  has a large component out of the solar equatorial plane; in this case, it is the  $\underline{e}_{\underline{B}} \times \underline{e}_{\underline{R}}$  direction that is the preferred one, and not the  $\underline{e}_{\underline{N}}$  direction. The fact that the average field direction frequently has significant components out of the equatorial plane explains why the R component of the fluctuations on the average has less power than the T component (Table 6),

since the  $\hat{e}_B \times \hat{e}_R$  direction never has a component along  $e_R$ , whereas it can easily have a component along  $e_T$  if  $e_B$  has a component along  $e_N$ . Earlier studies of Mariner 2 and Mariner 4 data [Coleman, 1967; Siscoe, 1968] have shown that the microscale field fluctuations are transverse to the average field direction with minimum power along  $e_R$ . These results are confirmed by the Mariner 5 data, and are seen to be a natural consequence of the frequent occurrence of transverse Alfvén waves partially polarized in the  $e_B \times e_R$  direction.

Alfvén waves convected into colliding stream regions will see a rapid change in the average field direction across the transition into the compressed plasma (see Figure 17). This more abrupt change in field direction (as compared to the gradual spiraling described above) should result in enhanced anisotropies and a higher level of (rapidly damped) magnetoacoustic oscillations, as observed. Another process suggested by J. R. Jokipii (private communication) that could contribute to the  $e_B \times e_R$  anisotropy in these regions is the probability that radially colliding streams produce primarily radial compressions and hence amplify magnetic fluctuations primarily normal to  $e_R$ . Those fluctuations along  $e_B \times e_R$  are pure Alfvén waves while those along  $e_R \times (e_B \times e_R)$  must become mixed Alfvénic and magnetoacoustic modes. The latter are rapidly damped, leaving the anisotropy and a higher plasma temperature.

The interpretation of the  $e_B \times e_R$  anisotropy as a result of magnetoacoustic wave damping has interesting implications with respect to the heating of the solar wind. The observational fact that the anisotropy extends over the entire microscale frequency range supports the conclusions of Jokipii and Davis [1969] that turbulence in the solar wind (such as in colliding stream regions) has no equilibrium subrange of wave numbers, in

contrast to ordinary turbulence. Instead of a cascade of energy to shorter and shorter wave numbers [Coleman, 1968], it appears that all wavelengths damp by direct interaction with the thermal plasma. The fact that this anisotropy is essentially always present implies that there is a continuous coupling between the dynamic microscale fluctuations and the thermal plasma which feeds energy out of wave motion and into thermal energy. We note also that the type of damping described above is essentially a geometrical coupling of Alfvén waves to the fast MHD mode propagating at a small angle with respect to the magnetic field (assuming  $\beta < 1$ ). Damping of the fast MHD mode at this angle increases the proton temperature parallel to the magnetic field by resonant Landau damping between the thermal protons and the wave [Barnes, 1966]. Since the observed Alfvén waves propagate predominantly outward, we would expect damping of the waves to heat thermal protons moving outward along the field lines, since it is these protons which resonate strongly with the waves. Thus, damping of the outwardly propagating Alfvén waves will contribute to the high energy tail of the proton thermal distribution [Hundhausen, 1967]. In the rest frame of the wind, the Alfvén waves transport energy outward at the rate  $V_A(\delta B)^2/8\pi$ , where  $\delta B$  is the wave amplitude and  $V_A$  is the Alfvén velocity. If we assume that the 5:4:1  $e_B x e_R$  anisotropy commonly observed at 1 a.u. means that 10 percent of the energy in the Alfvén waves at 1 a.u. has already been transferred by damping to the protons, we would expect to see an energy transport rate due to the high energy tail of the proton distribution of about  $10^{-5}$  ergs/cm<sup>2</sup> sec. for an Alfvén velocity of 50 km/sec and a wave amplitude of  $2\gamma$ . This is just the rate for the proton distribution found by Hundhausen [1967].

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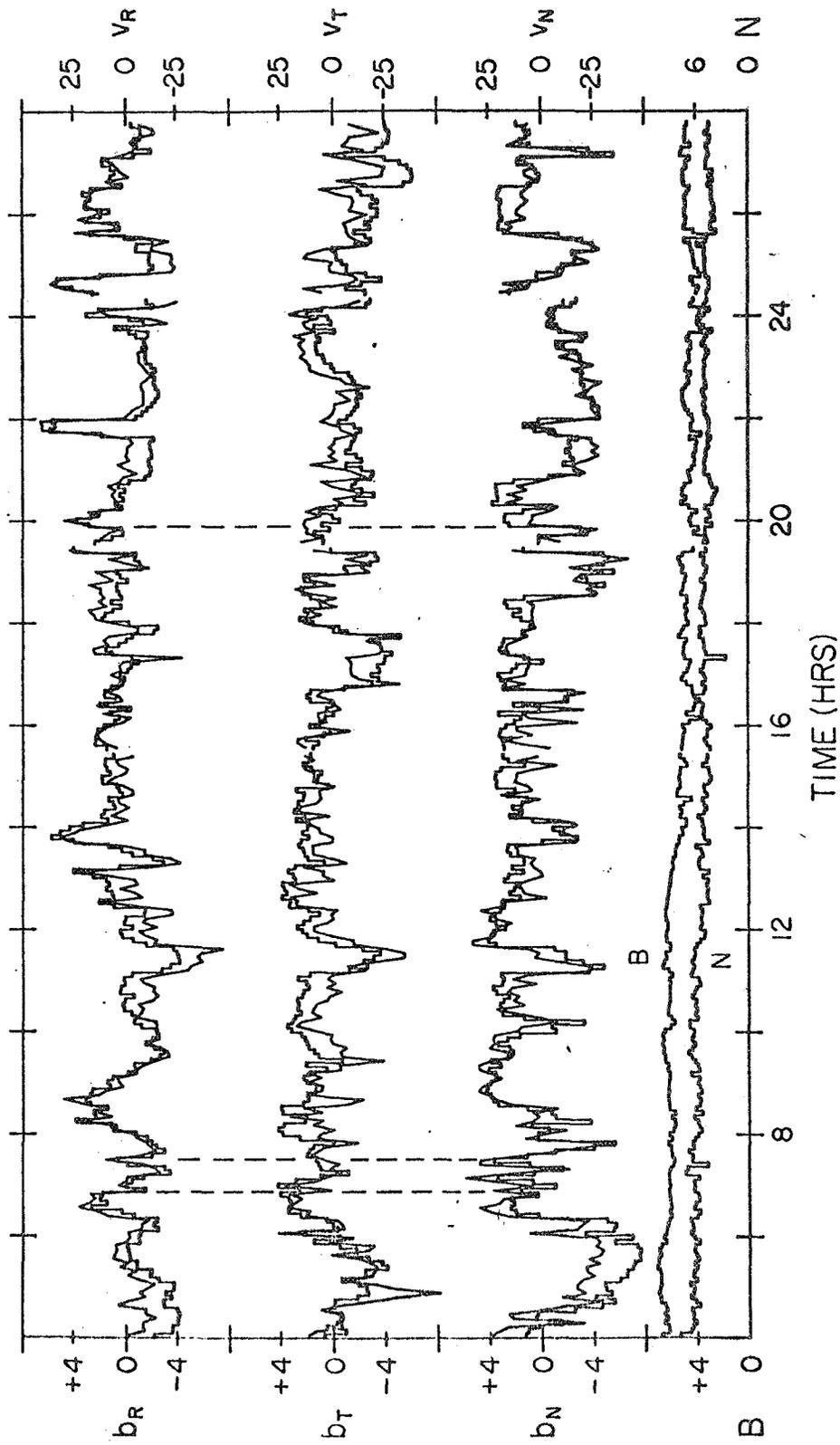


Figure 1. Twenty four hours of magnetic field and plasma data demonstrating the presence of nearly pure Alfvén waves. The upper six curves are 5.04 min. bulk velocity components in km/sec (diagonal lines) and magnetic field components averaged over the plasma probe sampling period, in gamma (horizontal and vertical lines). The lower two curves are magnetic field strength and proton number density.

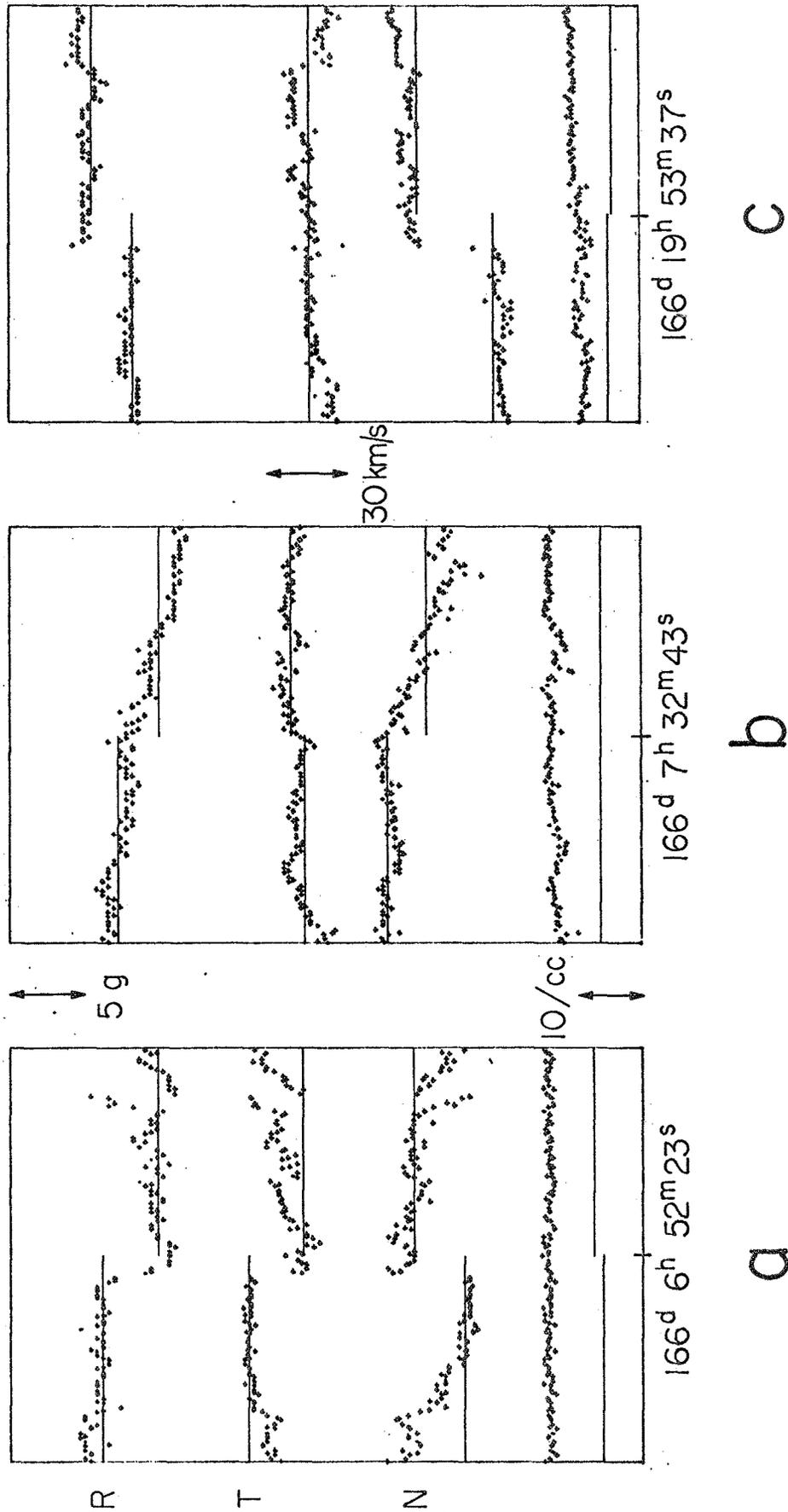


Figure 2. Expanded plots of three ten-minute intervals as indicated in Figure 1, showing the high frequency magnetic field fluctuations (crosses) and the 5.04 minute plasma readings (bars). The lower two curves are field strength and proton number density, and the upper six are bulk velocity and field components.

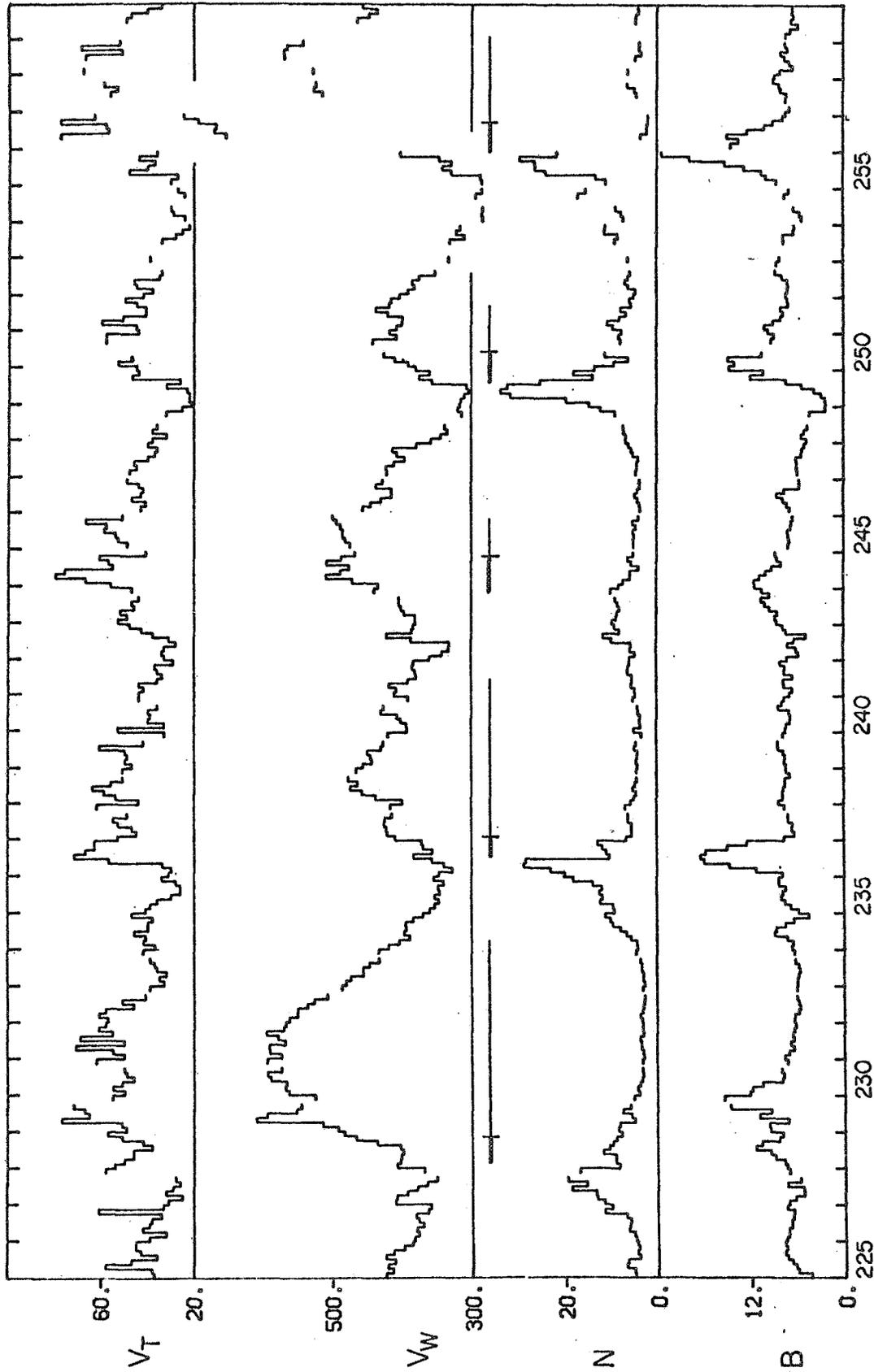


Figure 3. 35 days of Mariner V data plotted using three hour averages and showing the large scale stream structure of the solar wind. B is the magnetic field strength ( $\gamma$ ), N is the proton number density ( $\text{cm}^{-3}$ ),  $V_W$  is the radial proton bulk velocity (km/sec), and  $V_T$  is the most probable proton thermal speed (km/sec). The best examples of the outwardly propagating Alfvén waves (light bars) are found in high velocity streams and on their trailing edges. The largest amplitude waves (heavy bars) are found at the leading edges of high velocity streams.

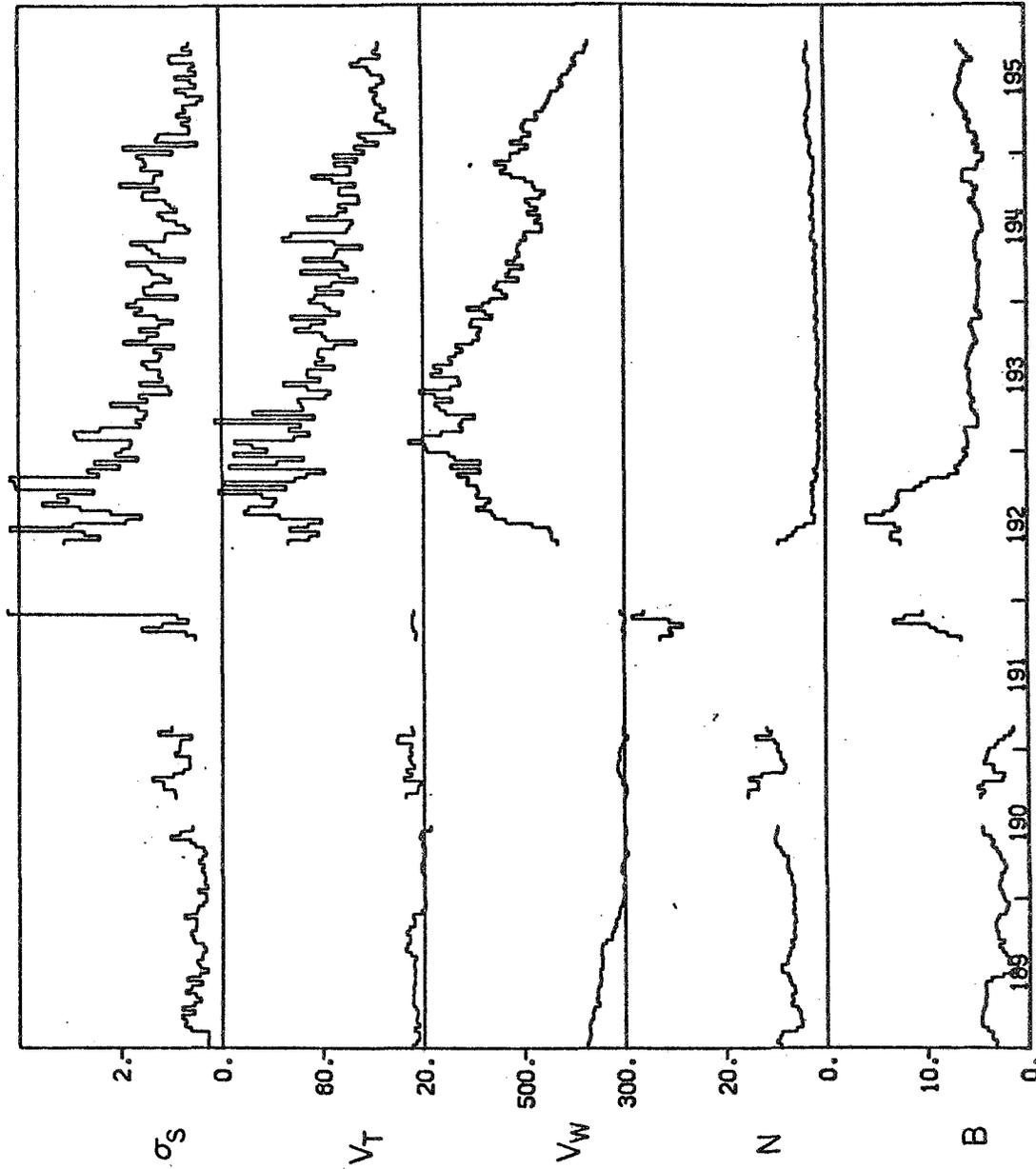


Figure 4. 7 days of Mariner V data plotted using 40.4 minute averages and showing a detailed stream-stream interaction. B, N,  $V_W$ , and  $V_T$  are as in Figure 3, and  $\sigma_S(y)$  is the square root of the average over 40.4 minutes of the sum of the variances over 5.04 minutes of the R, T, and N components of the field.

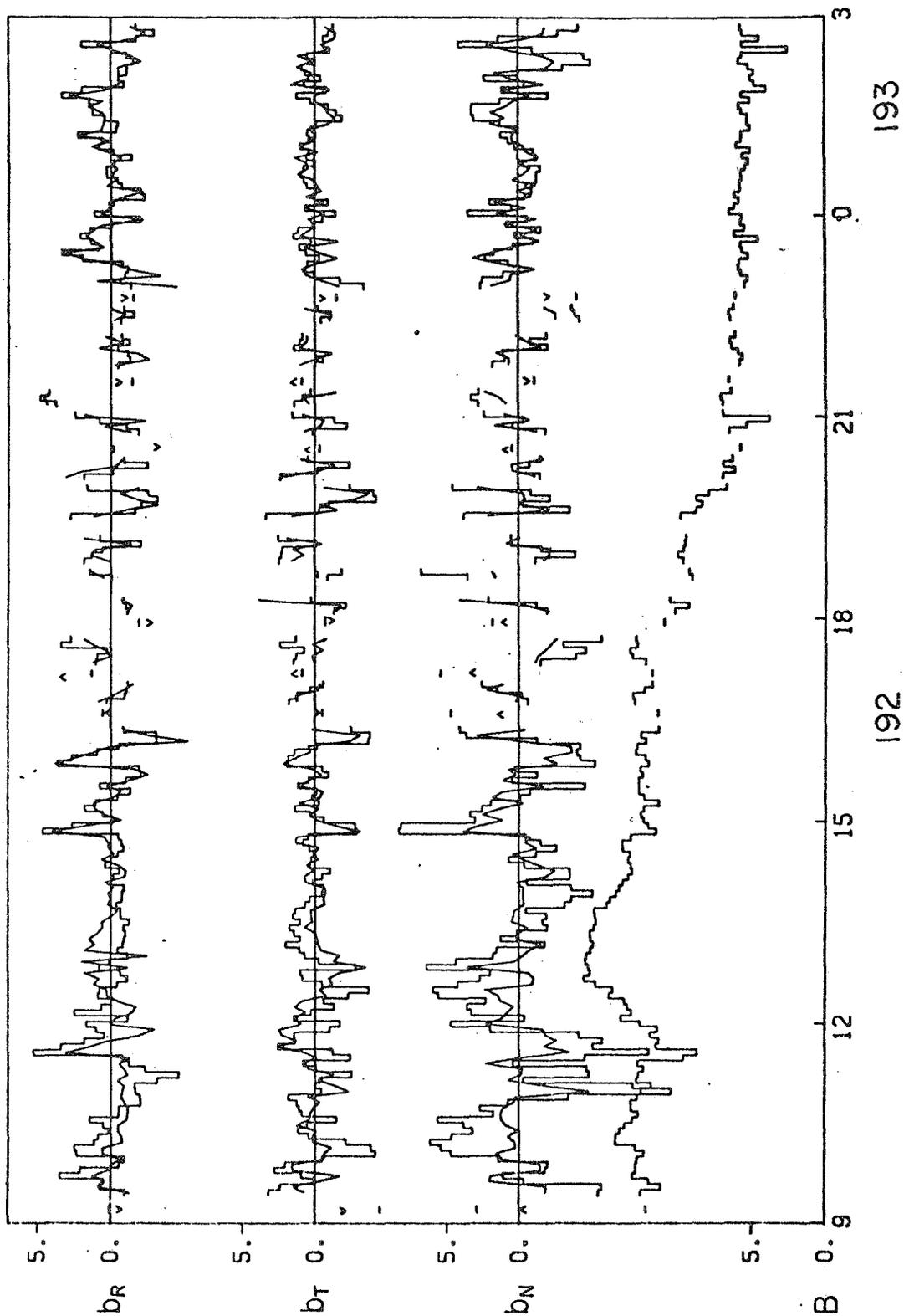


Figure 5. 5.04 minute measurements of the magnetic field strength B and the field components (horizontal and vertical lines) and bulk velocity components in units of gamma (diagonal lines) for a 18 hour period of Figure 4. Variations with periods longer than two hours have been filtered from all curves except B; B here is the magnitude of the 5.04 minute average field vector.

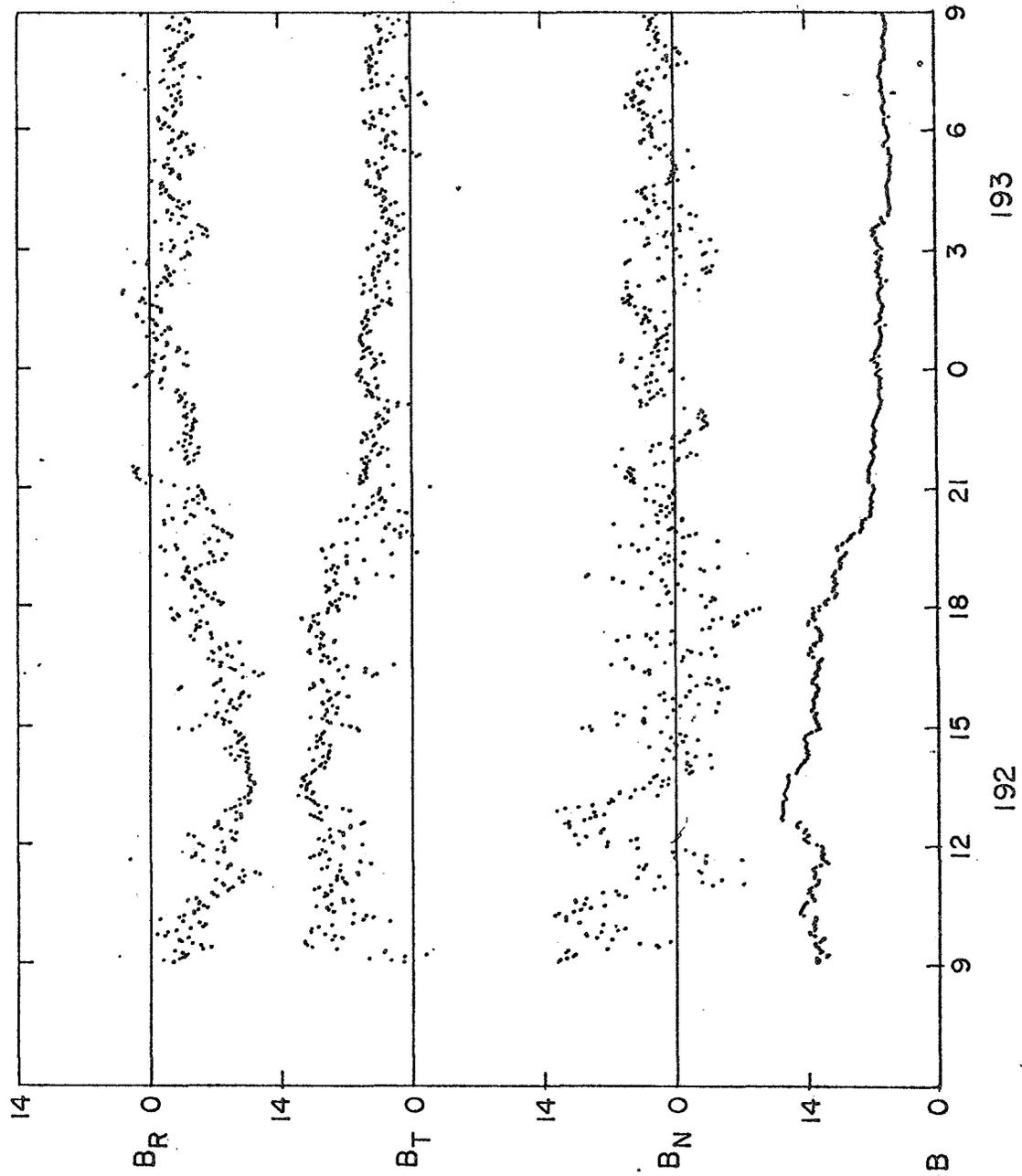


Figure 6. 168.75 second averages of field components and magnitude plotted over a 24 hour period of Figure 4. Field strengths given here are averaged magnitudes, and thus have more physical significance than those in Figure 5, where the magnitude of averaged field vectors is plotted. Note the increase in wave amplitude as the compression region is entered.

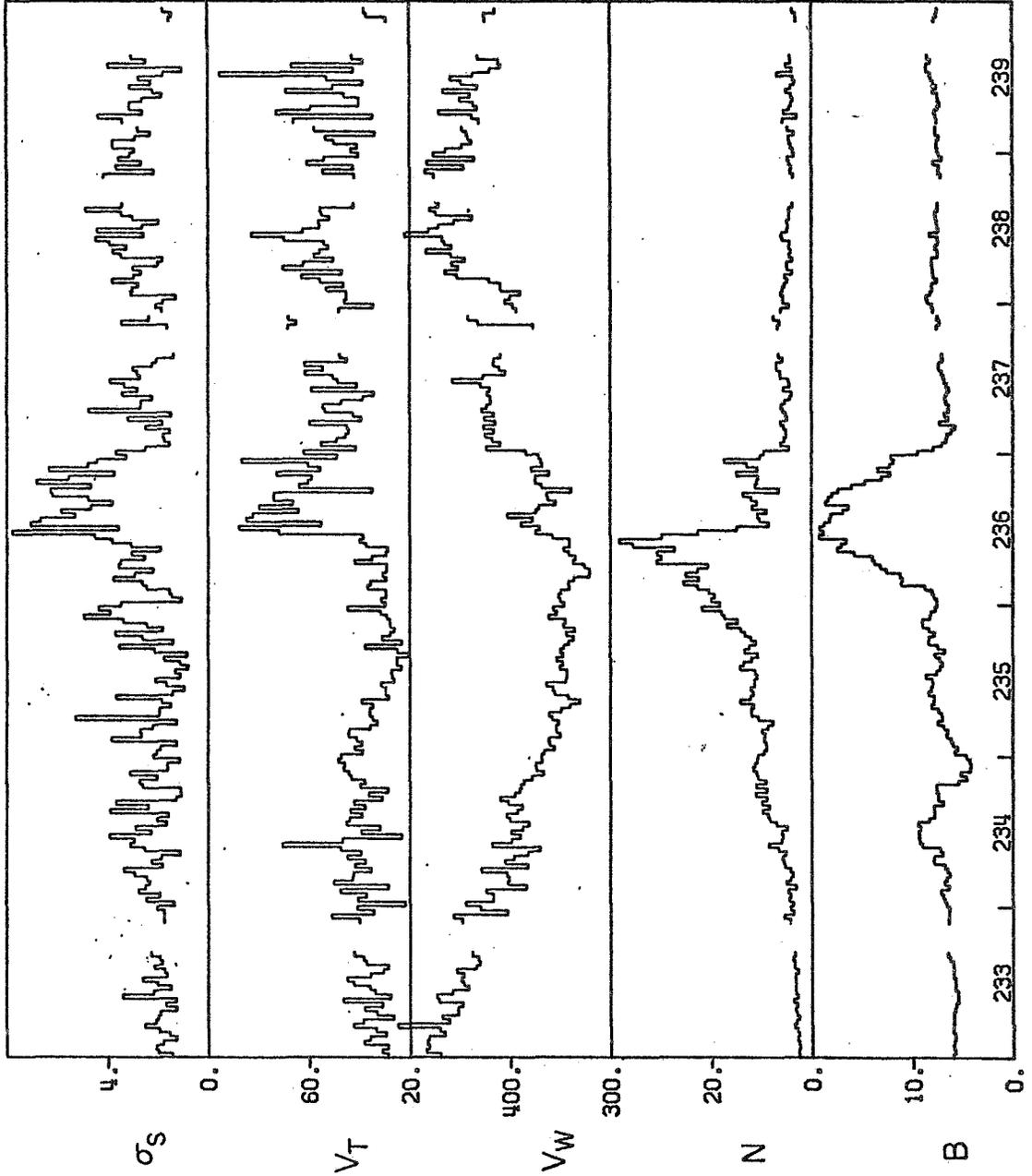
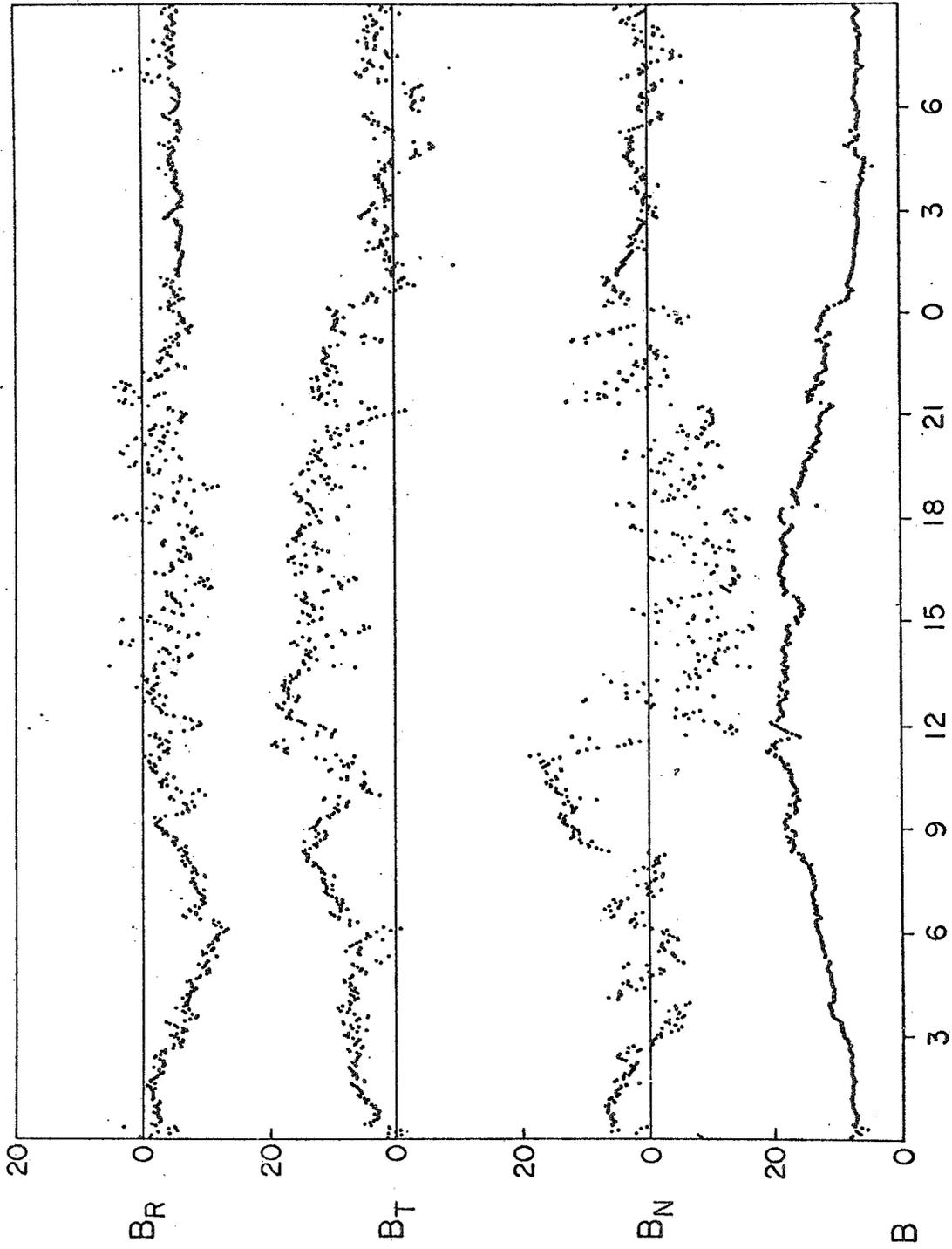


Figure 7. A low data rate example of detailed stream structure using 40.4 minute averages, similar in format to Figure 4. Here  $\sigma_S$  is the square root of the averaged 20.2 minute total variance in field components. Note the high values of  $\sigma_S$  and  $V_T$  in the latter half of day 236.



237

236

Figure 8. 168.75 second averages of field components and magnitude plotted over a 33 hour period of Figure 7, similar to Figure 6. The large wave amplitudes with high normal power in the latter half of day 236 are characteristic of colliding stream regions.

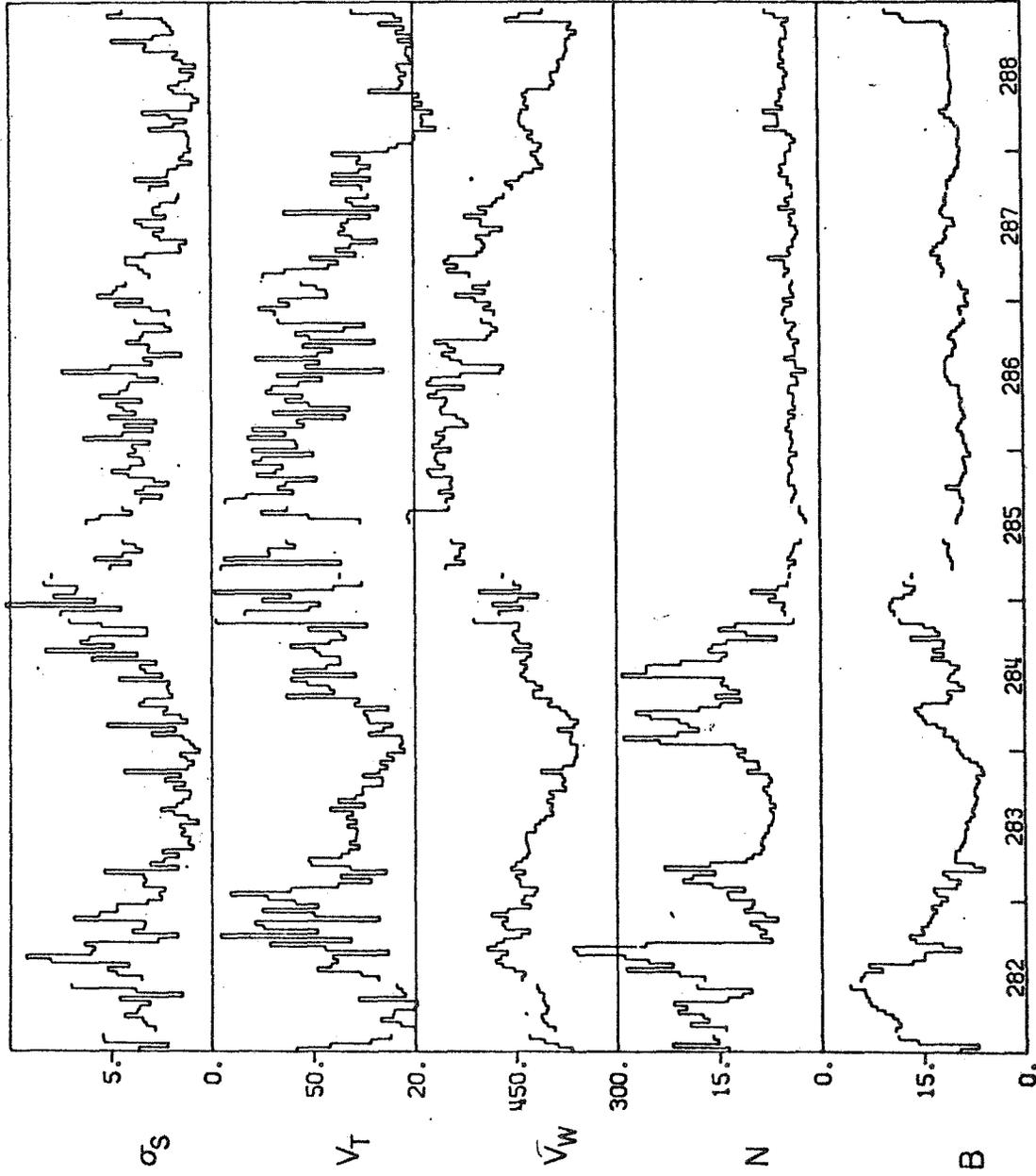


Figure 9. An example of detailed stream structure using 40.4 minute averages, similar in format to Figure 7. The situation ahead of the fast stream (before day 284) is chaotic.

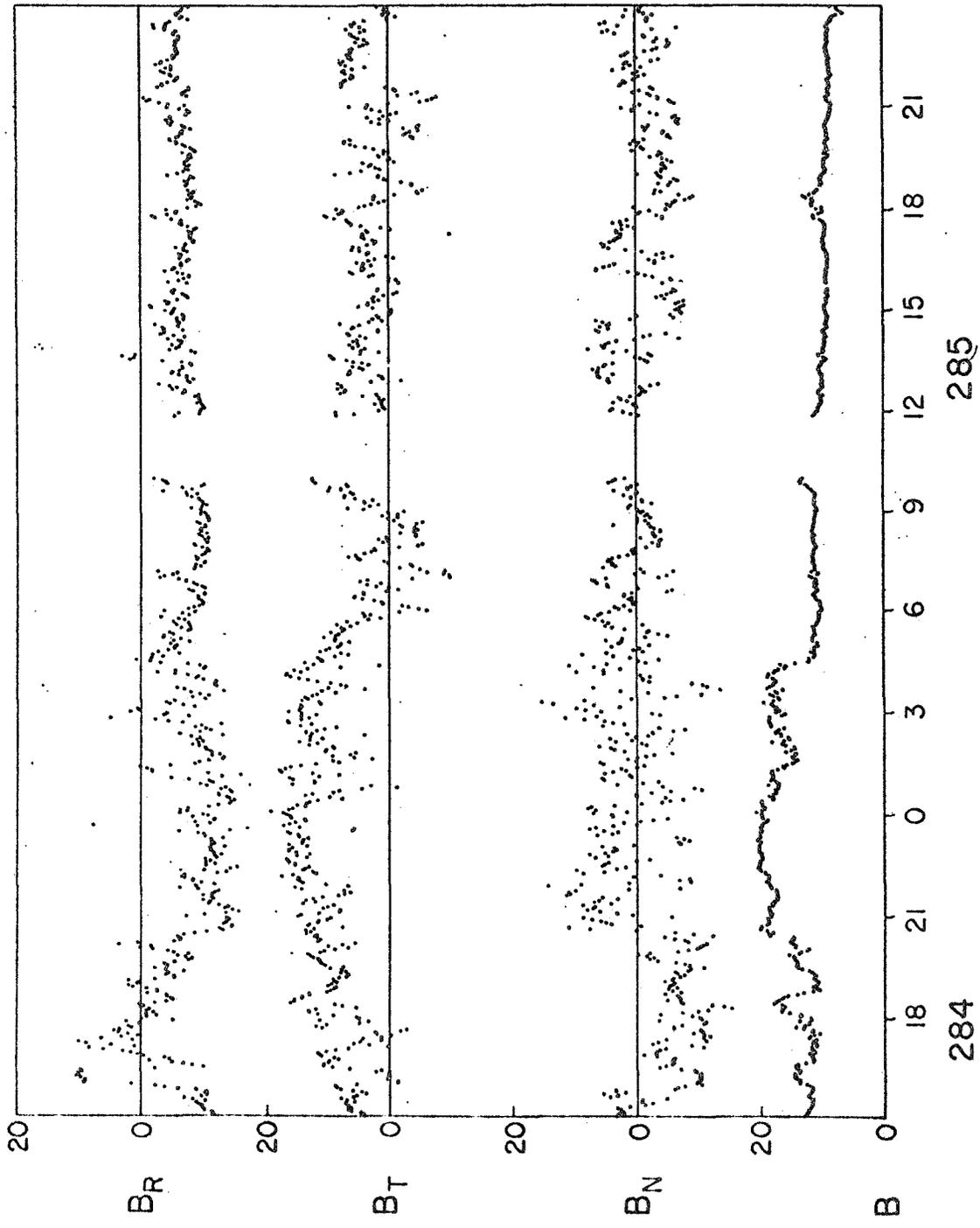


Figure 10. 168.75 second averages of field components and magnitude plotted over a 33 hour period of Figure 9, similar to Figure 6. Note the abrupt increase in wave amplitude as the compression region is entered.

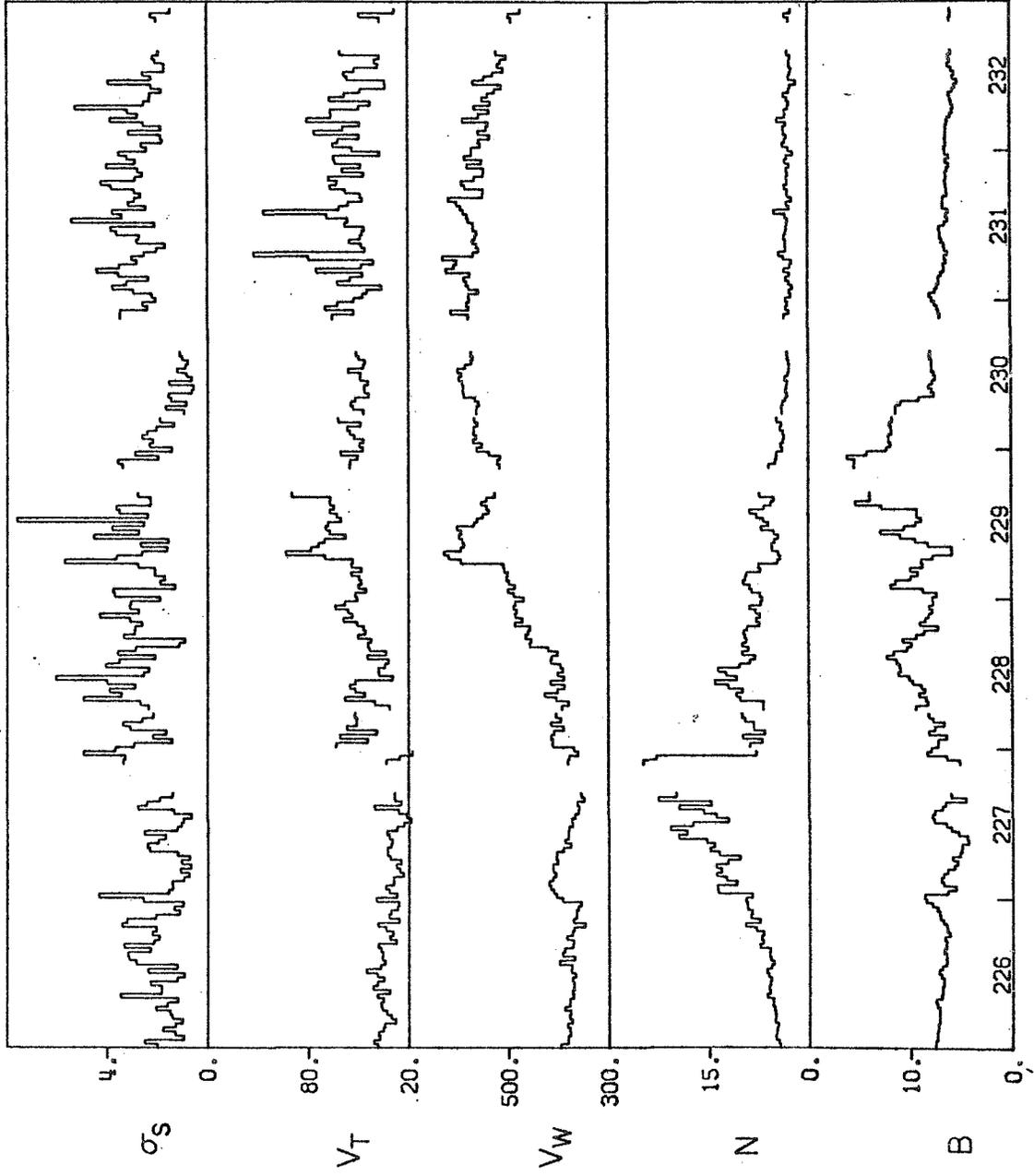


Figure 11. An example of detailed stream structure using 40.4 minute averages, similar in format to Figure 7. The velocity gradient region extends from the beginning of day 228 into day 229.

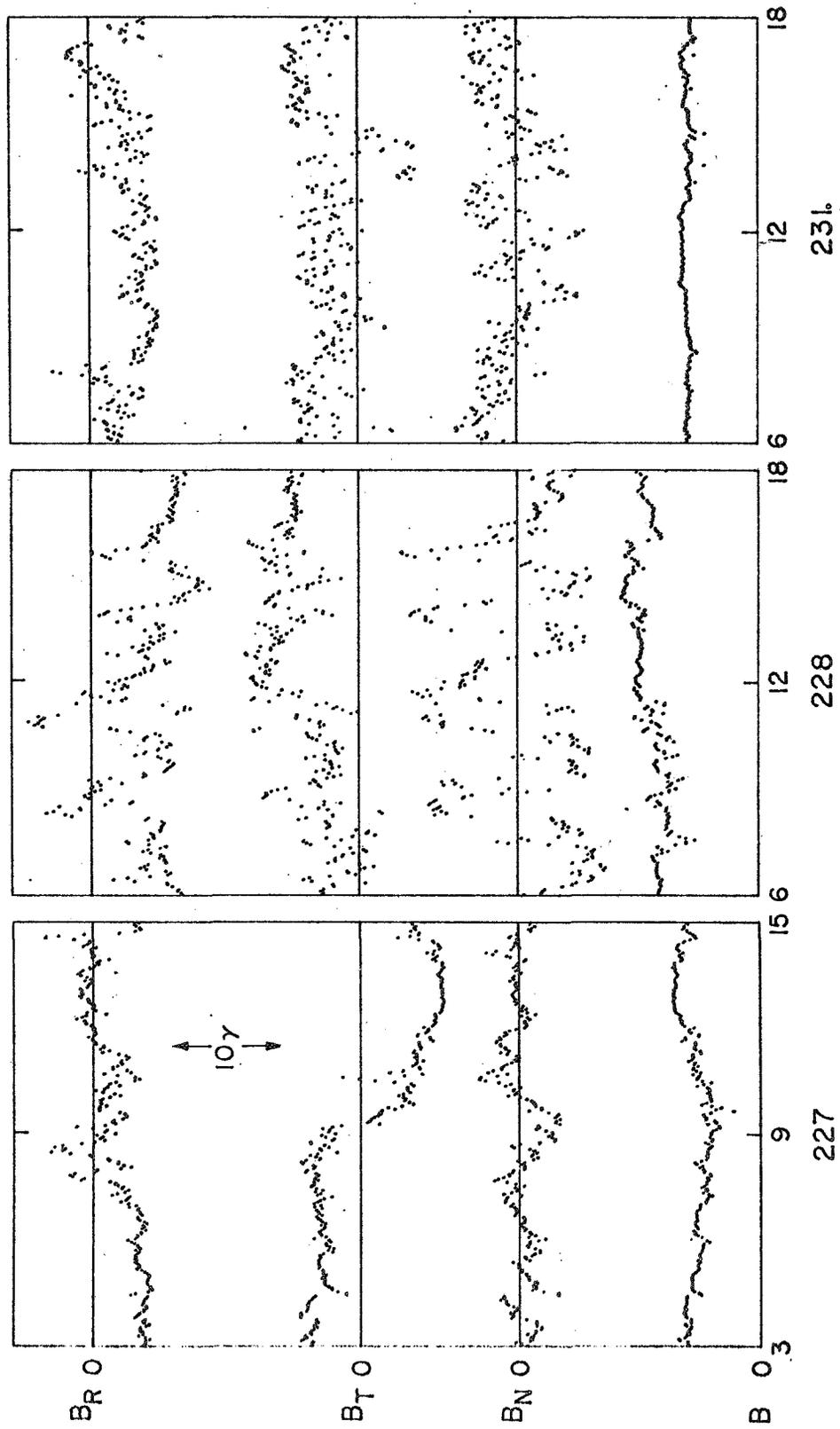


Figure 12. 168.75 second averages of field components and magnitude plotted for three twelve-hour periods of Figure 11, showing field fluctuations characteristic of low velocity streams, compression regions, and high velocity streams, respectively.

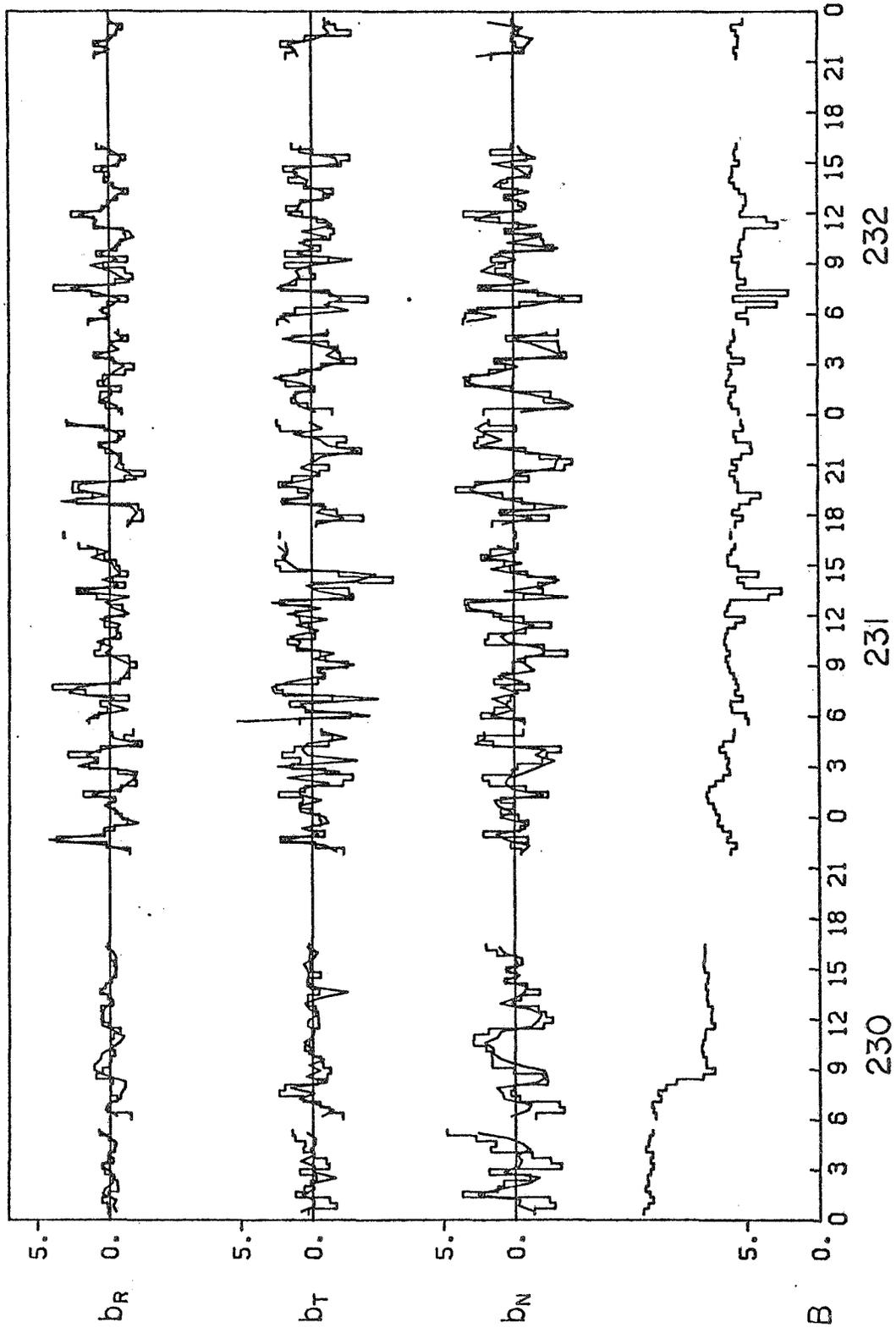


Figure 13. Magnetic field strength  $B$  and field and bulk velocity components for a three day period of Figure 11, similar in format to Figure 5. Each point represents a 20.2 minute measurement, and variations with periods longer than four hours have been subtracted from all curves except  $B$ . As in Figure 5,  $B$  is the magnitude of the averaged field vector, so that it is only approximately the averaged magnitude of the field.

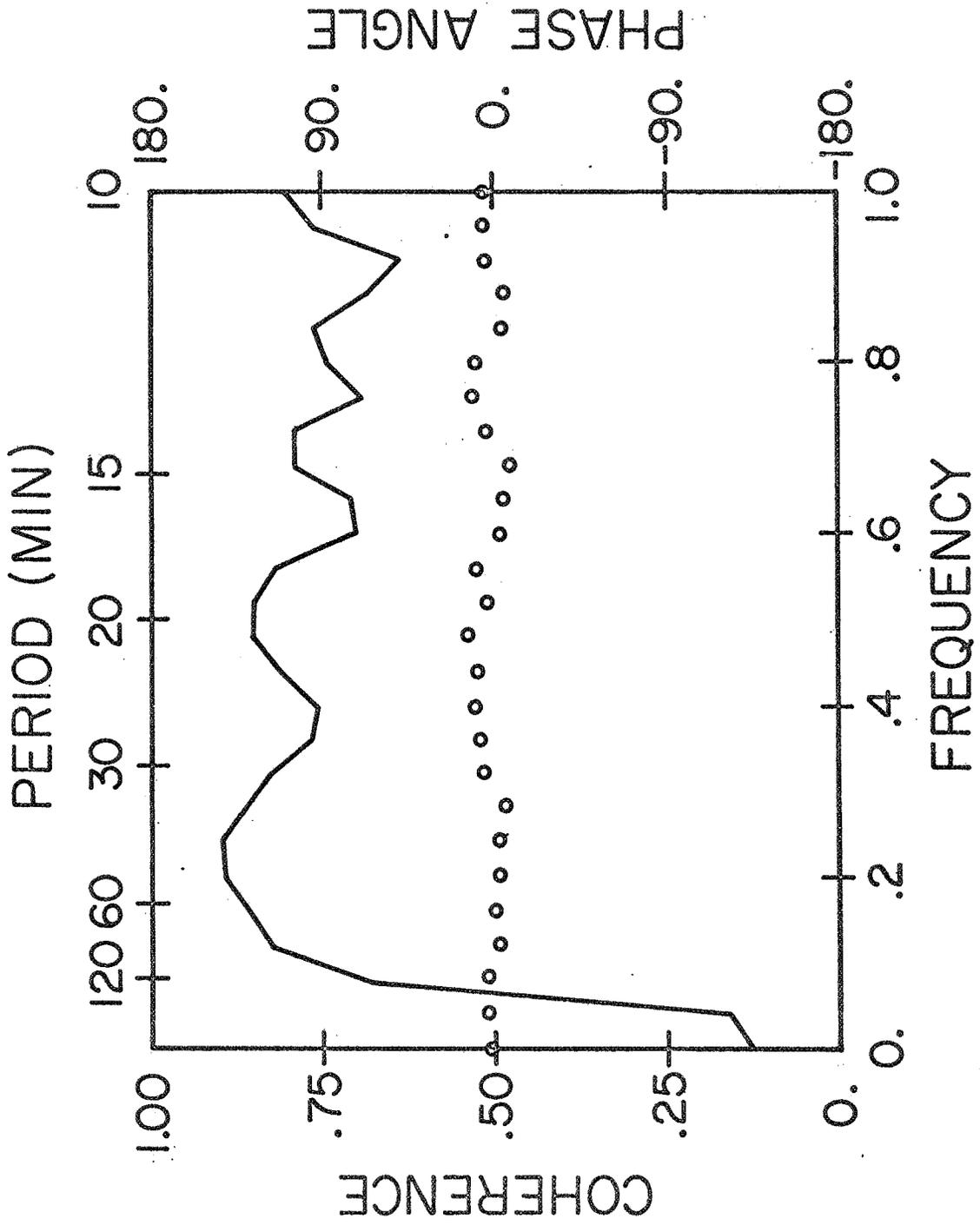


Figure 14. Coherency (line) and phase (circle) estimates for cross spectra between  $V_R$  and  $B_R$  during a period of good Alfvén waves (193-194), computed with 30 degrees of freedom.

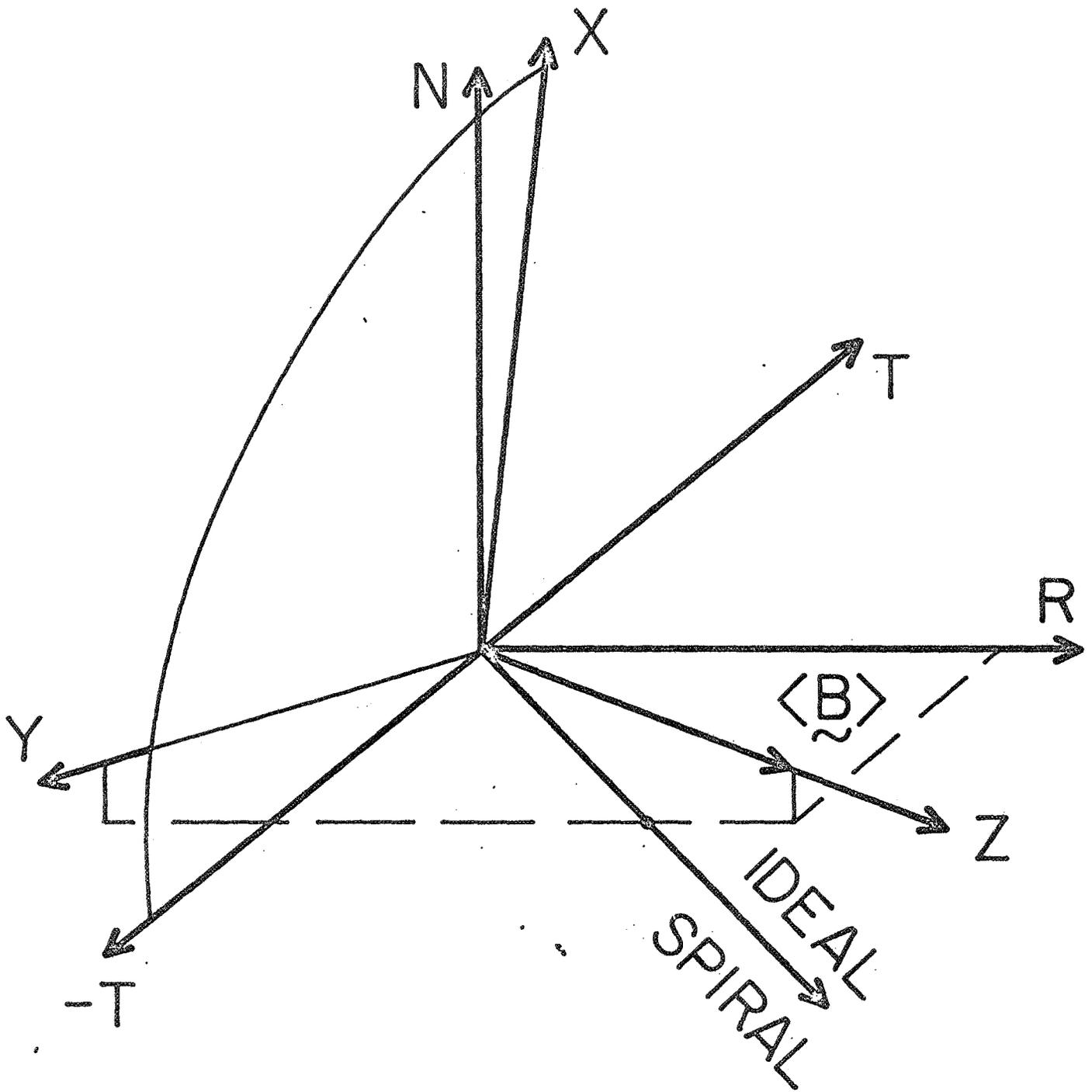


Figure 15. The field-velocity coordinate system. Z is along the average field direction, and X is along  $\tilde{z} \times \tilde{e}_R$ . The X-axis thus always lies in the TN plane.

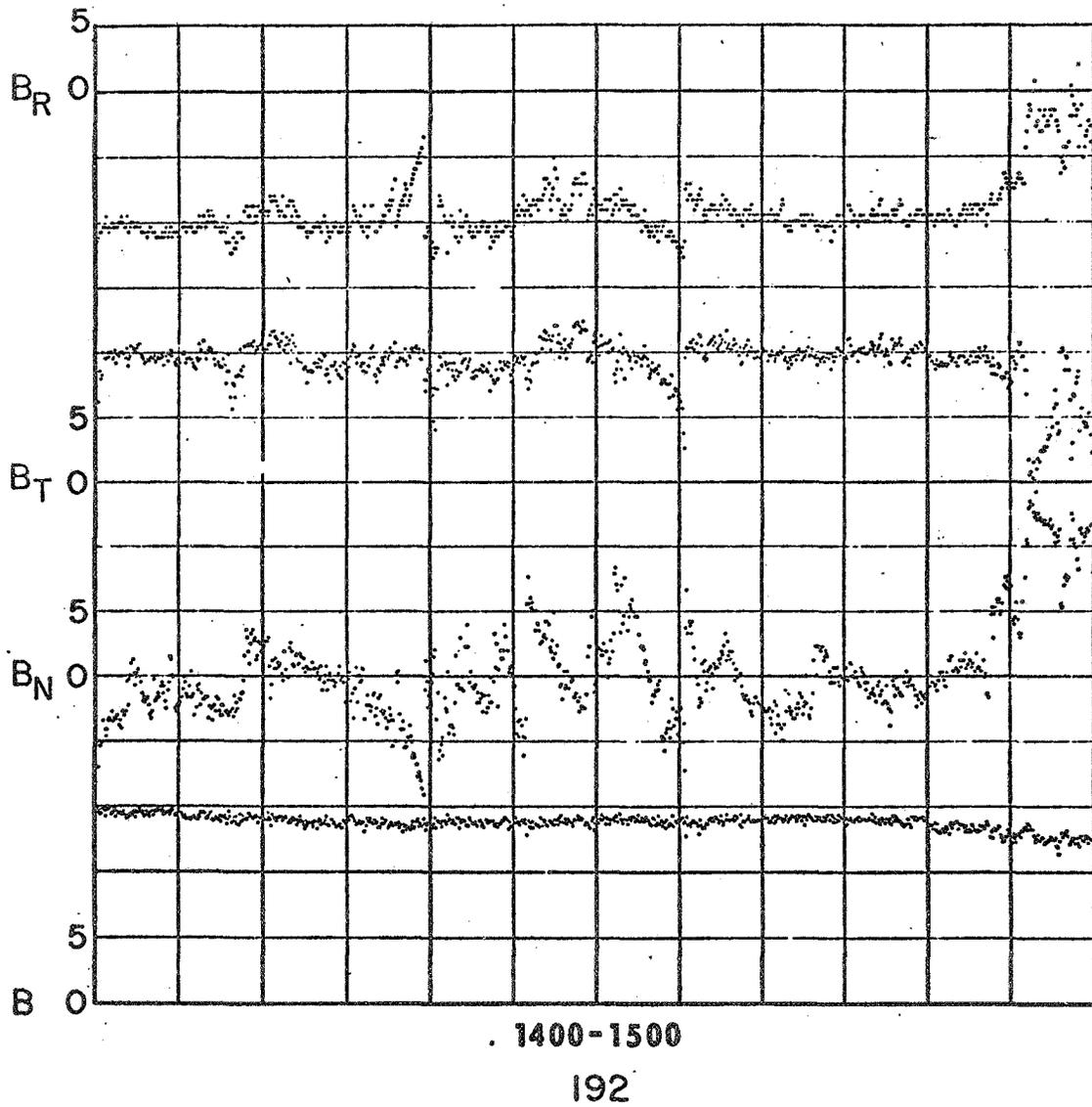


Figure 16. High frequency magnetic field fluctuations during a one hour period of day 192 showing clearly the large amount of power in the N direction. The data shown is basic magnetometer data, with one reading in approximately 4 seconds.

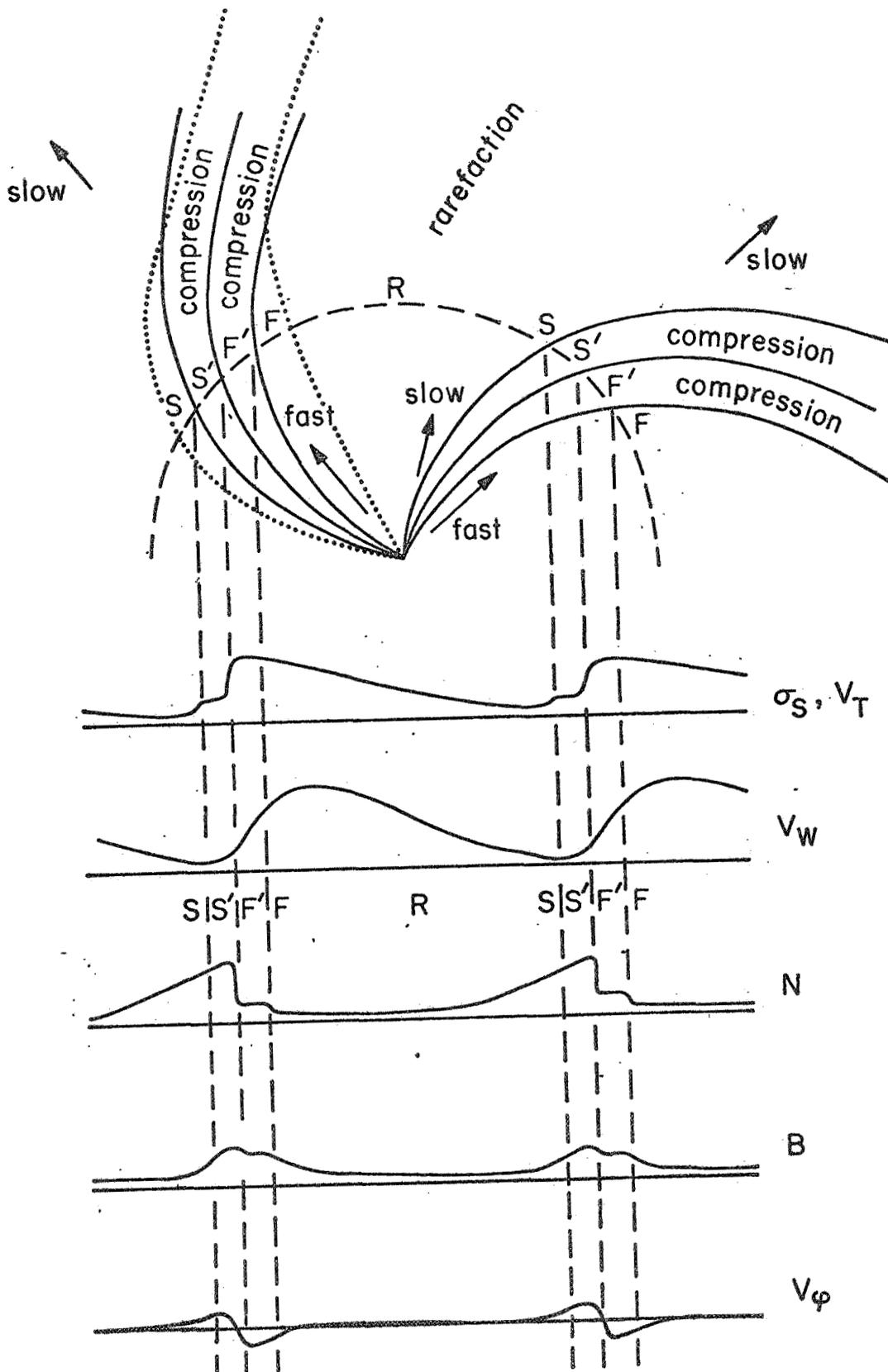


Figure 17. Top half, two high velocity streams and adjacent low velocity streams shown at one instant for the steady state case. Dotted lines represent ideal spiral magnetic field lines and are also the flow lines for the steady state flow in the corotating frame. Bottom half, curves showing as functions of time the changes in solar wind parameters which will be observed by a spacecraft as the streaming pattern sweeps past.  $\sigma_T$ ,  $V_T$ ,  $V_W$ ,  $N$ , and  $B$  are as defined above, and  $V_\phi$  is the T component of the solar wind velocity.